

# Forecast sensitivities for the Medicane of 7 November 2014. Dynamical vs Statistical methods

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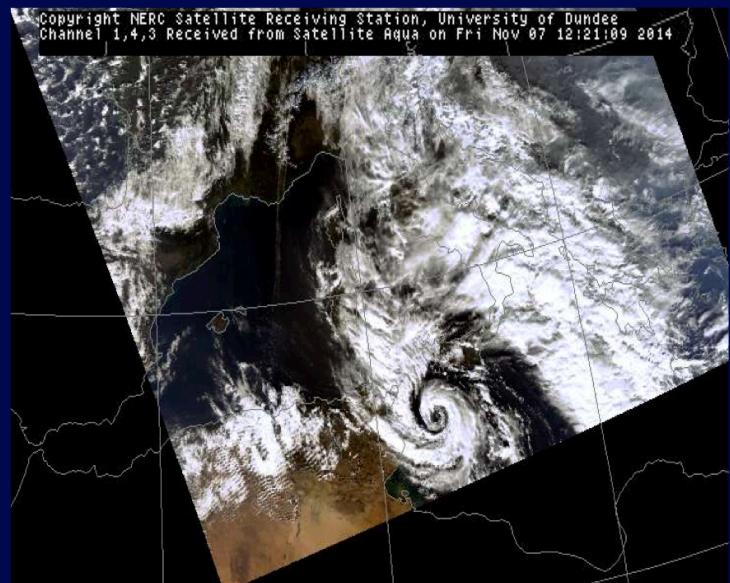
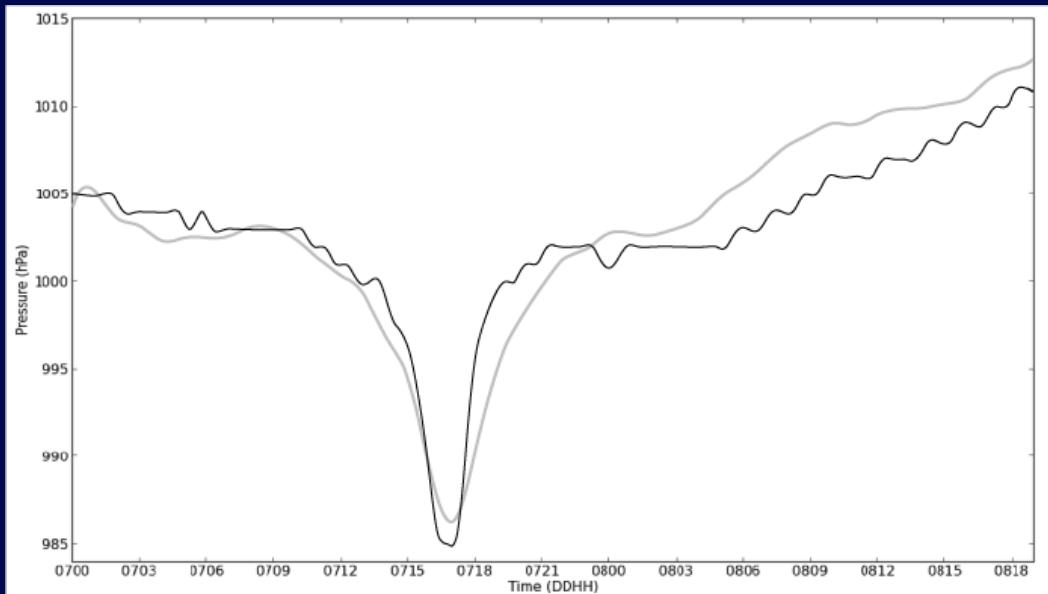
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# The case study

November 7<sup>th</sup>, 2014 (causes and effects also on 5<sup>th</sup>, 6<sup>th</sup> and 8<sup>th</sup>)

Affects Tunisia, Malta, Lampedusa and Sicilia.

Drop of over 20hPa in 6h in Malta, wind gusts of over  $42.7 \text{ ms}^{-1}$ .



# Introduction to sensitivities

(Statistical) ensemble sensitivities      Adjoint sensitivities

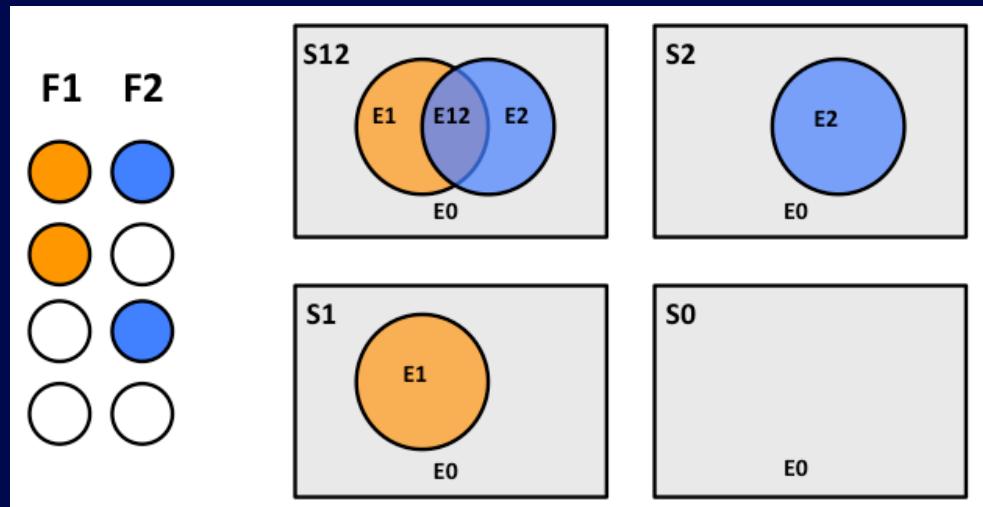
Factors separation

$$E0 = S0$$

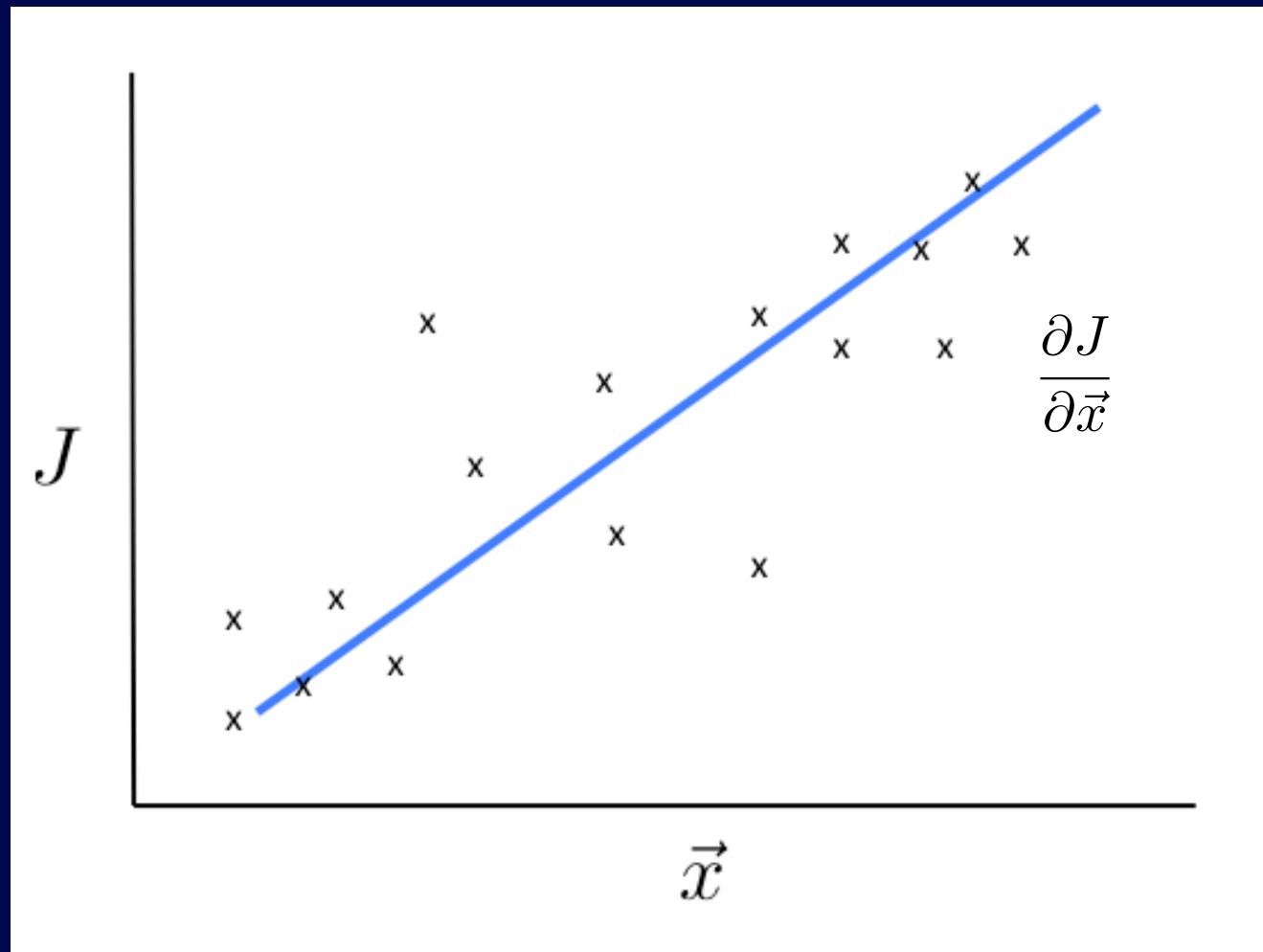
$$E1 = S1 - S0$$

$$E2 = S2 - S0$$

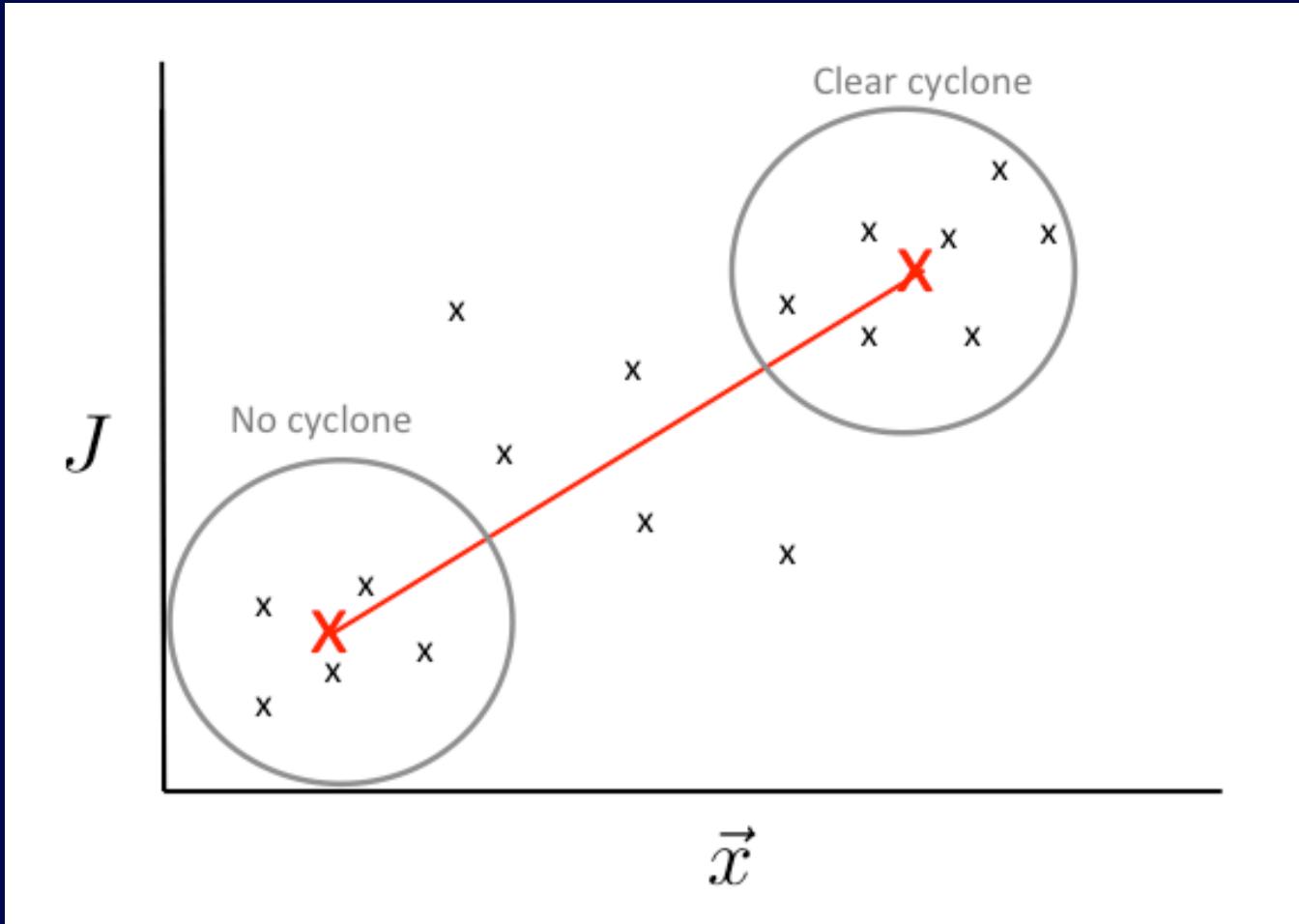
$$E12 = S12 - (S1 + S2) + S0$$



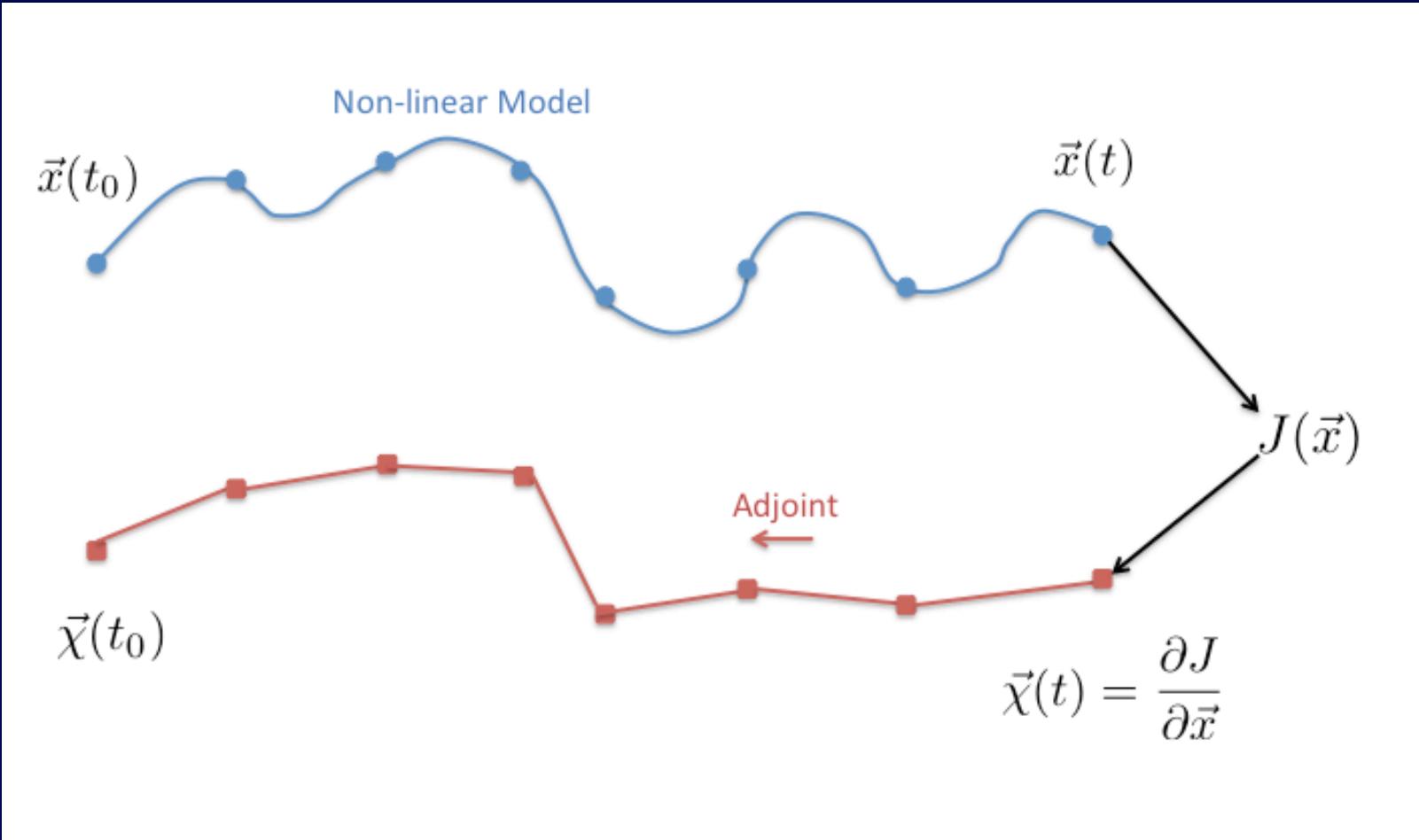
# Ensemble sensitivities



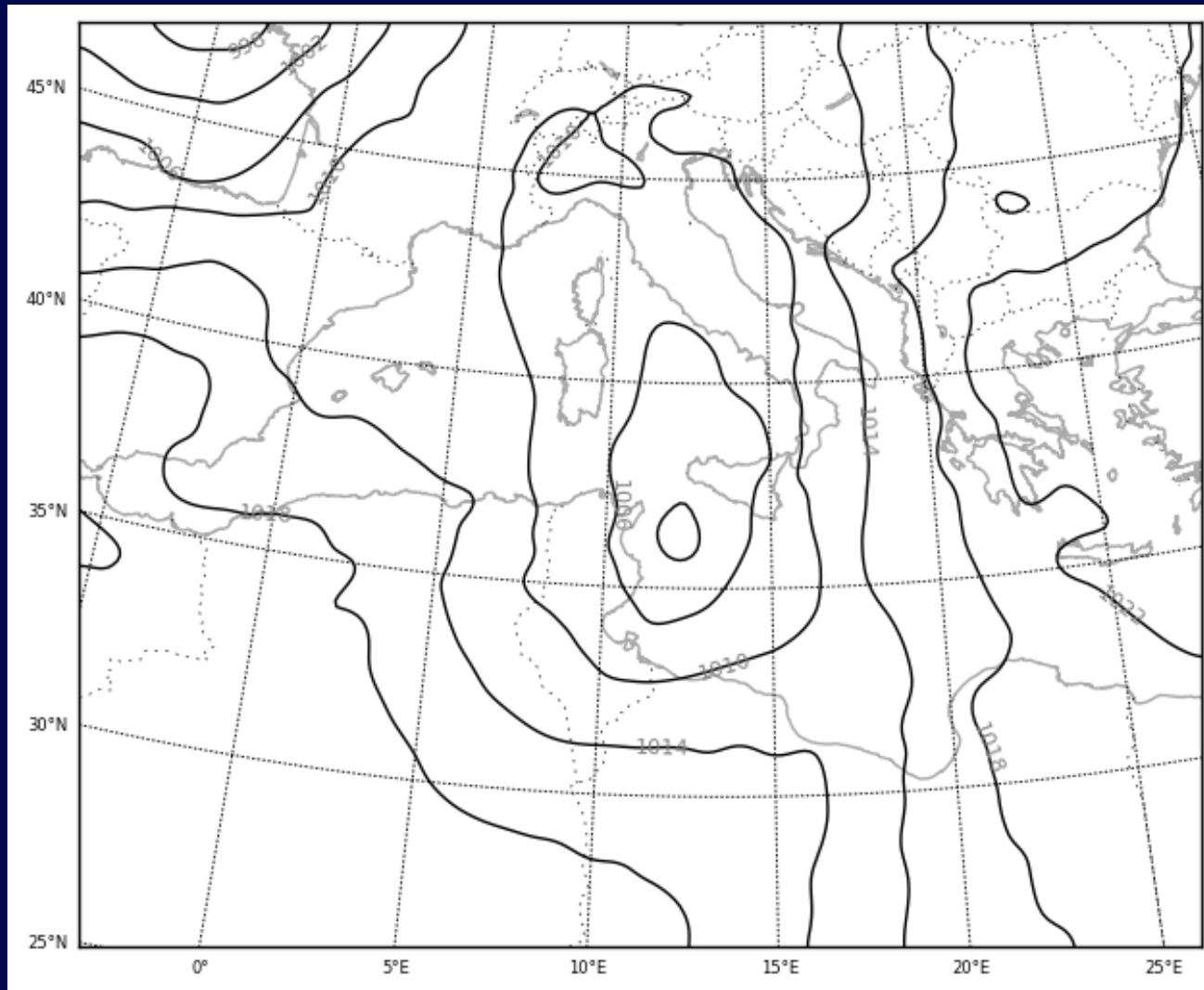
# Clustered ensemble sensitivities



# The adjoint model

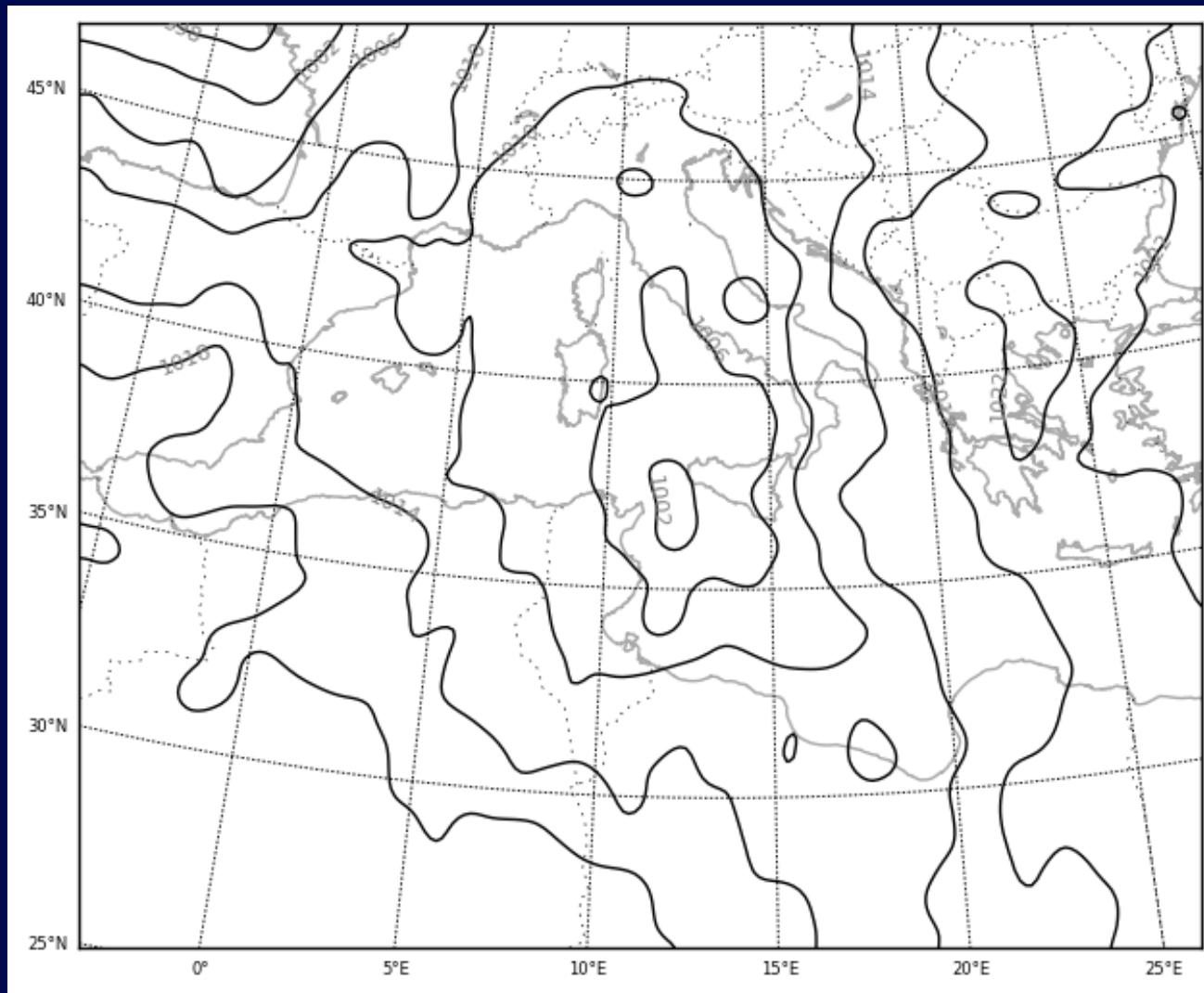


# The evolution of the sea level pressure



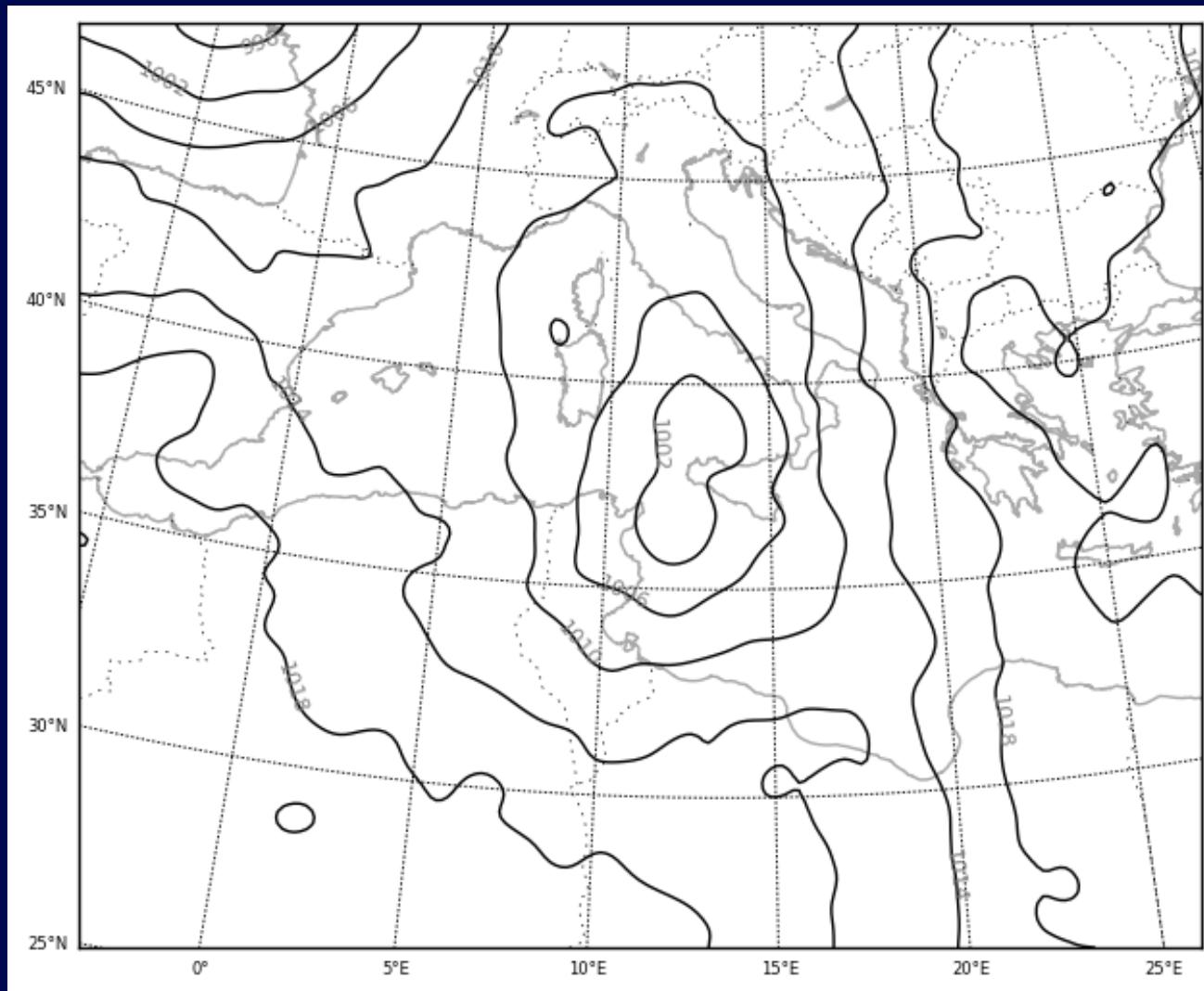
Time index: 0

# The evolution of the sea level pressure



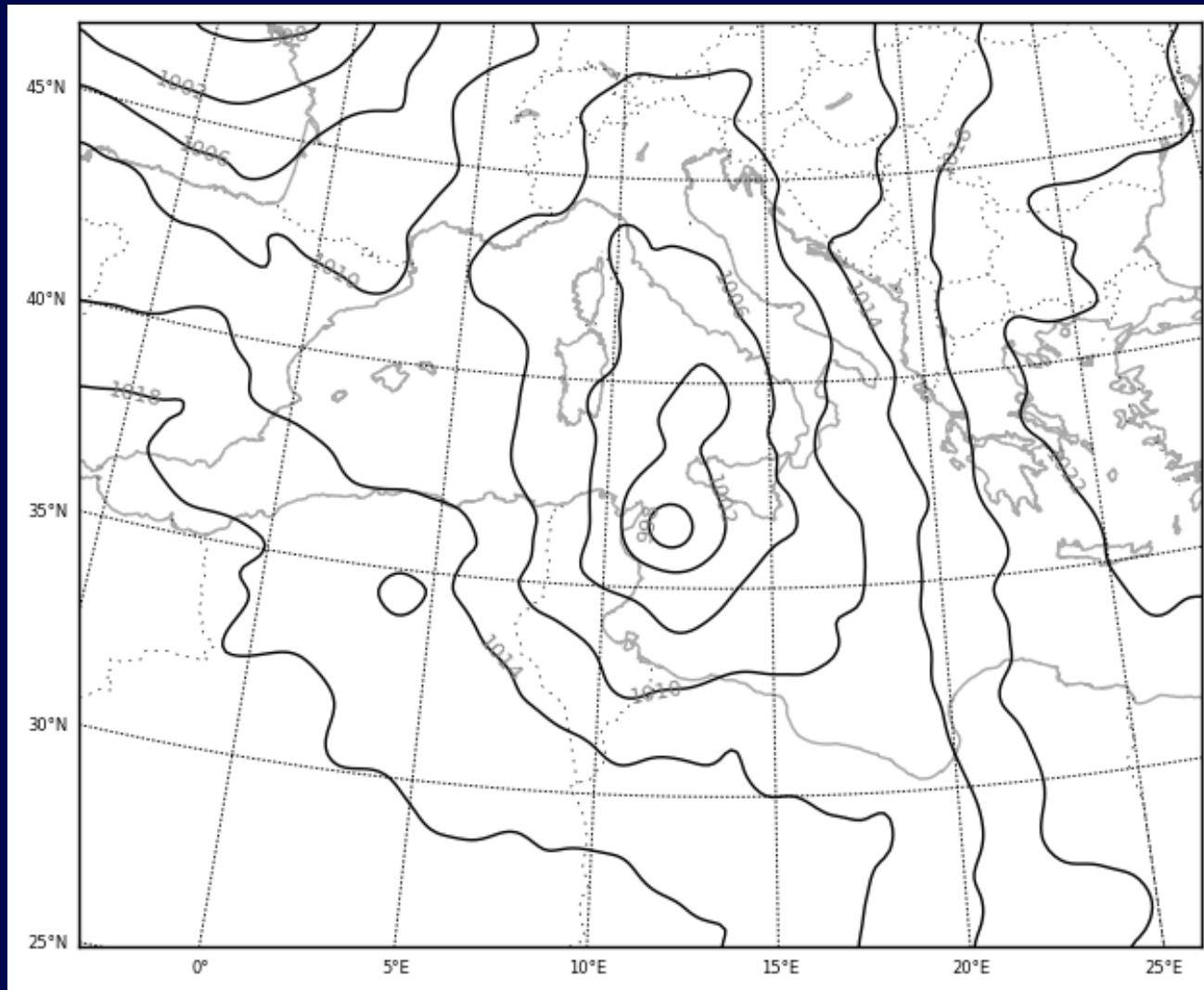
Time index: 1

# The evolution of the sea level pressure



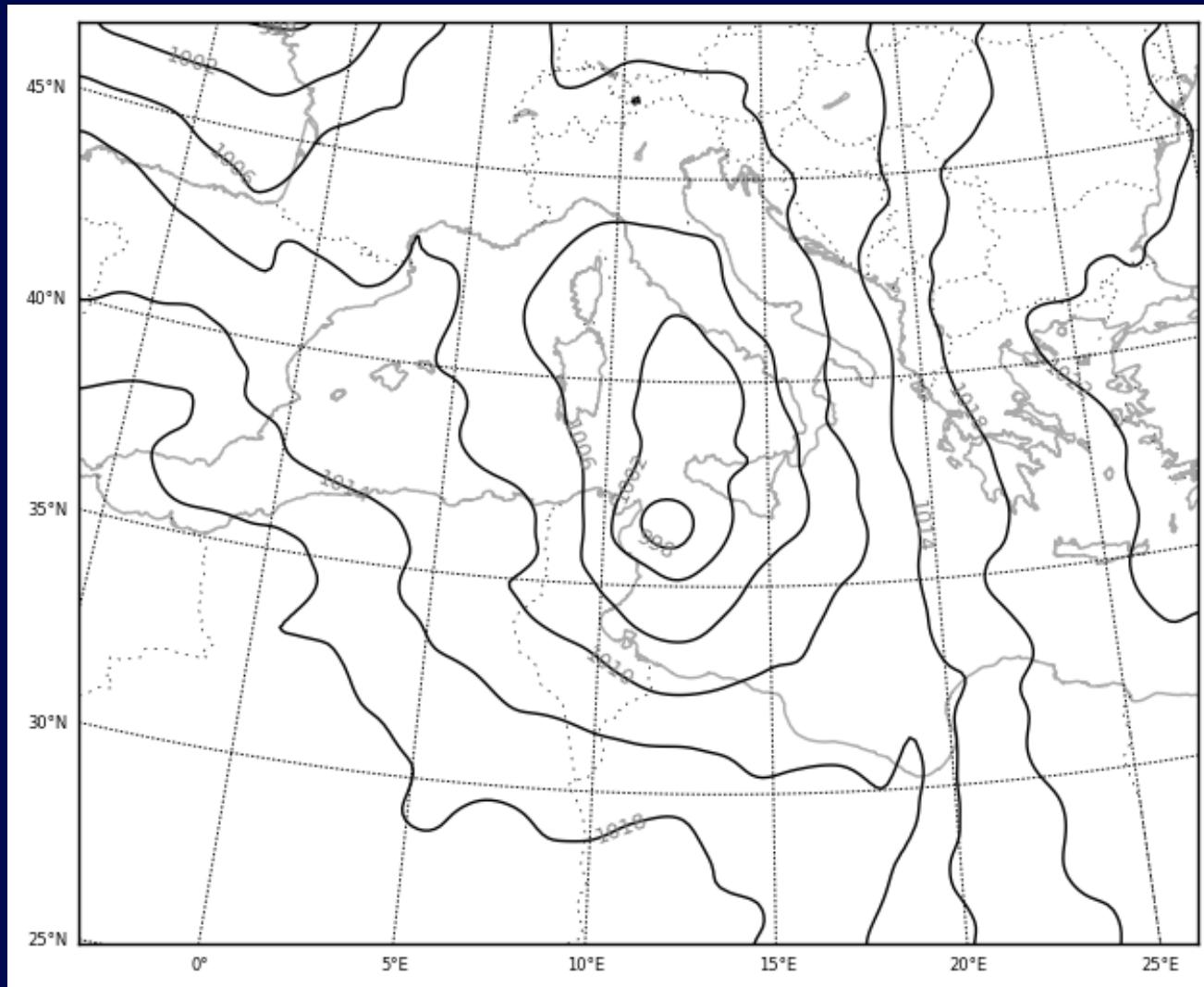
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# The evolution of the sea level pressure



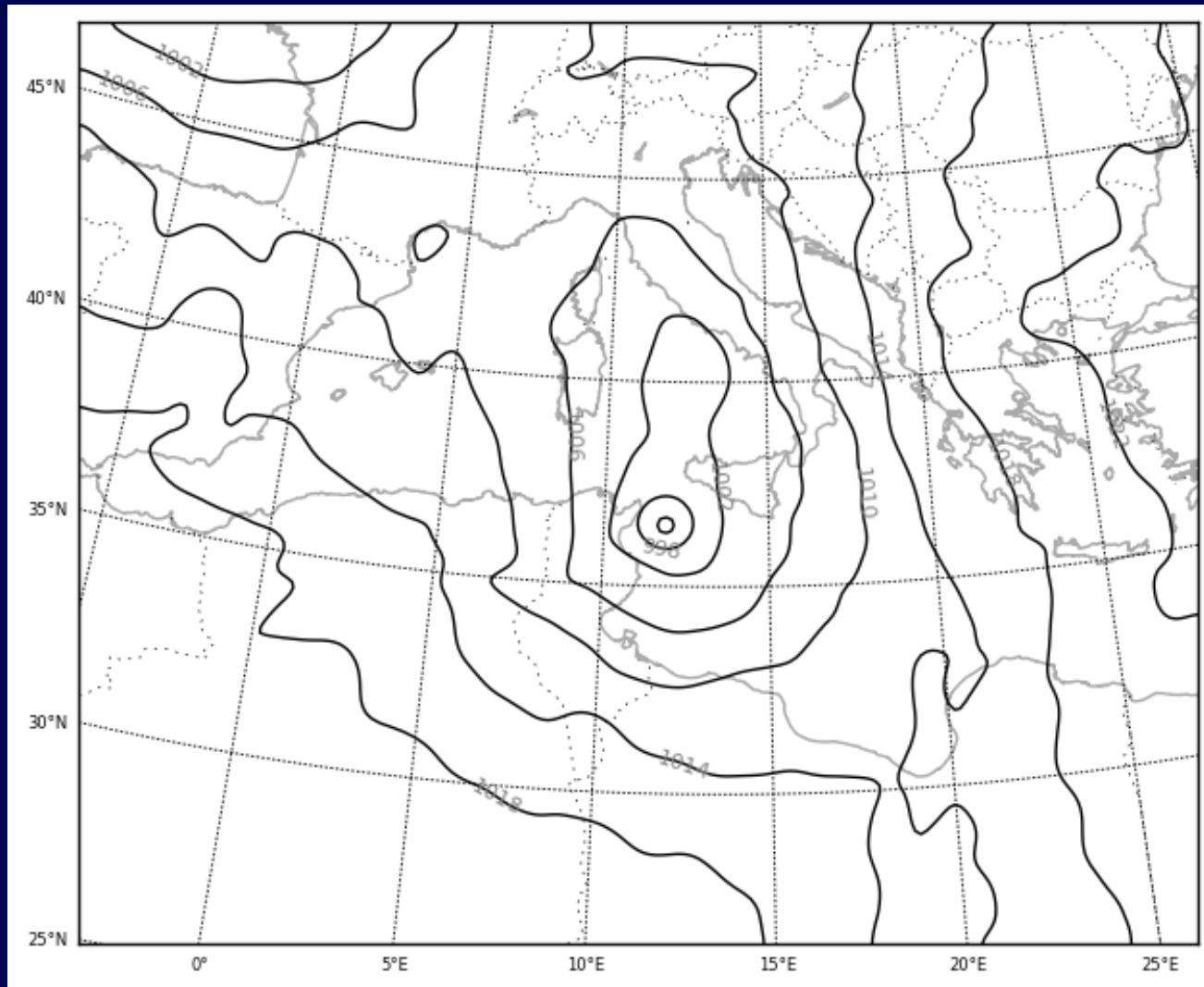
Time index: 3

# The evolution of the sea level pressure



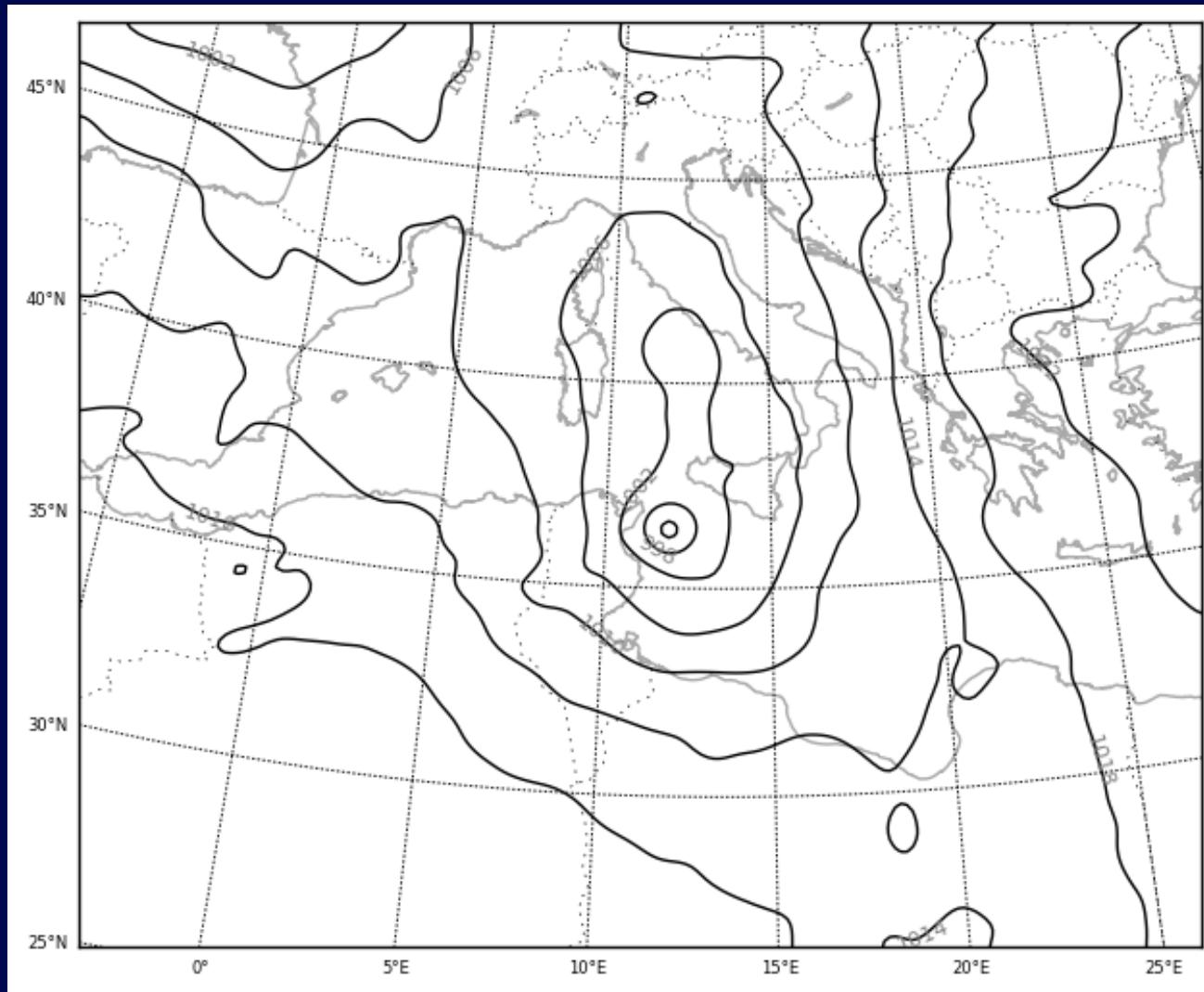
Time index: 4

# The evolution of the sea level pressure



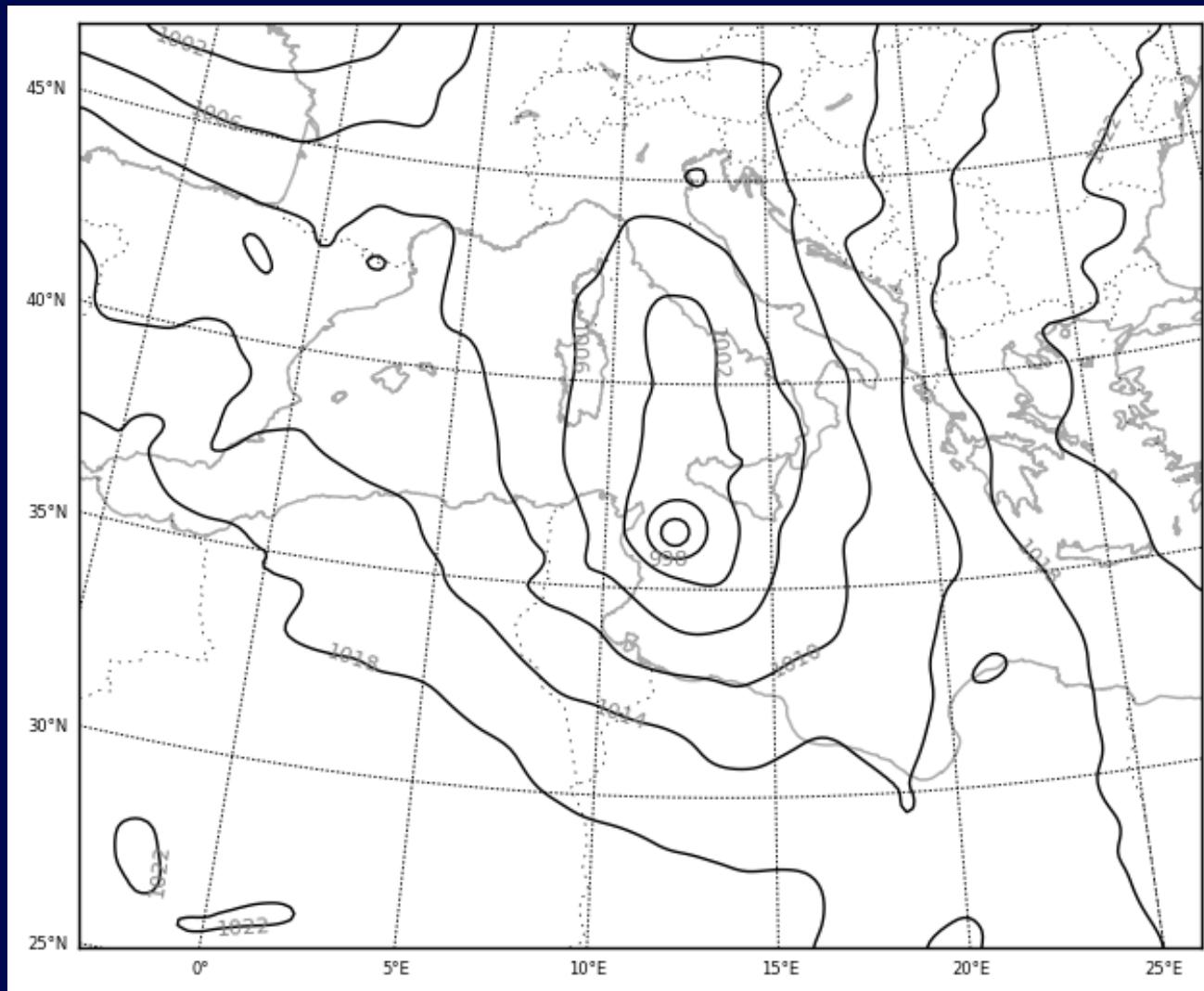
Time index: 5

# The evolution of the sea level pressure



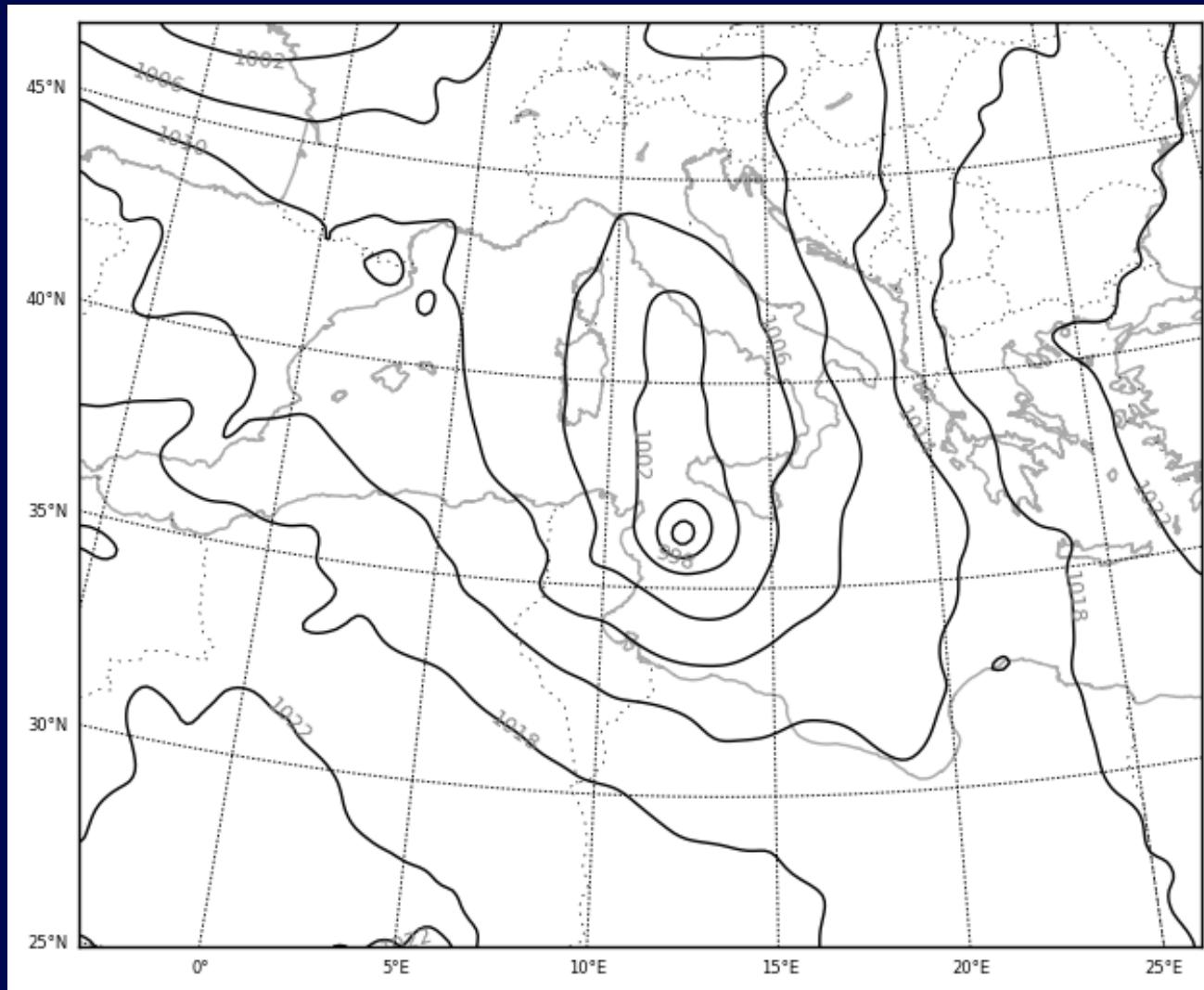
Time index: 6

# The evolution of the sea level pressure



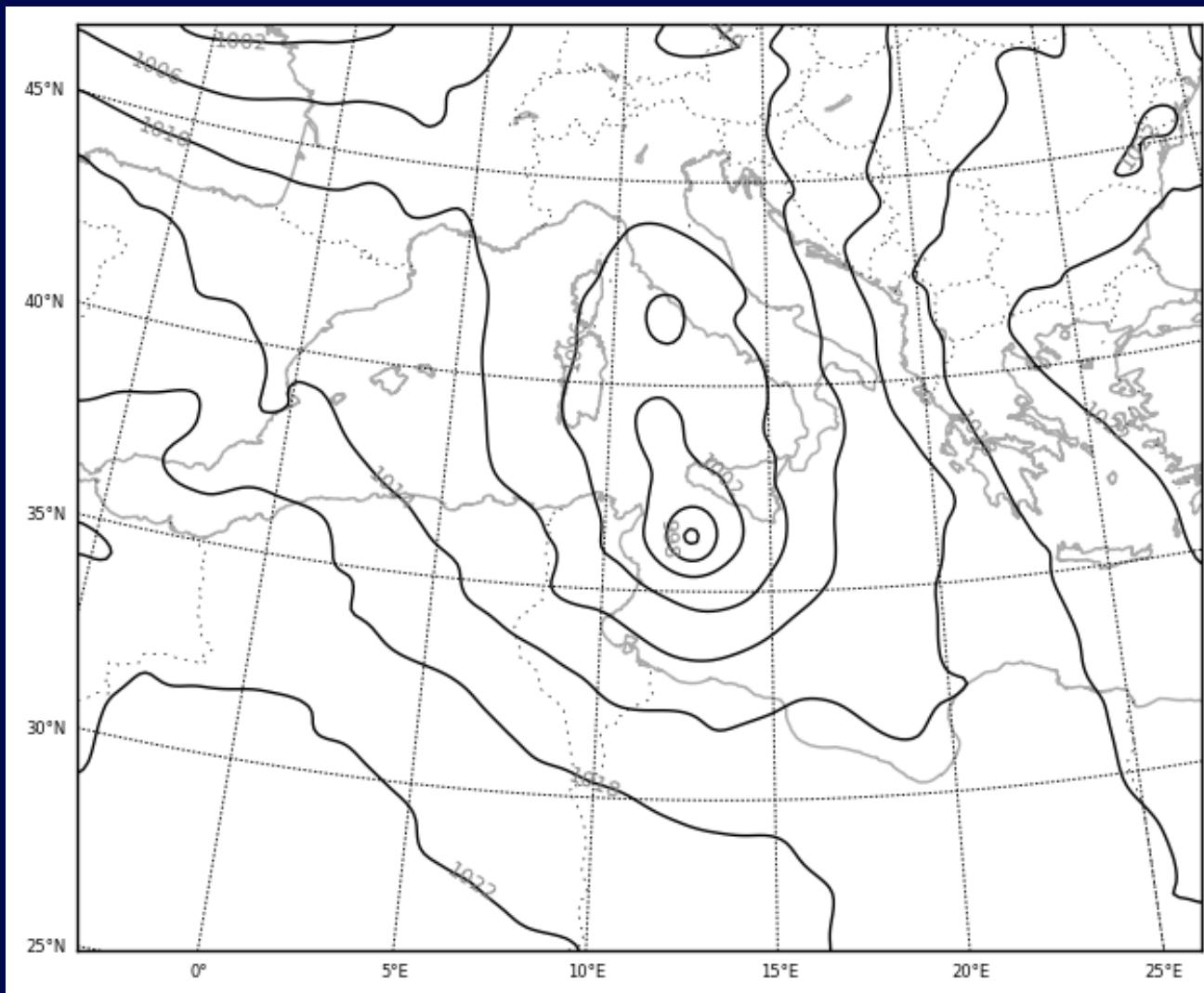
Time index: 7

# The evolution of the sea level pressure



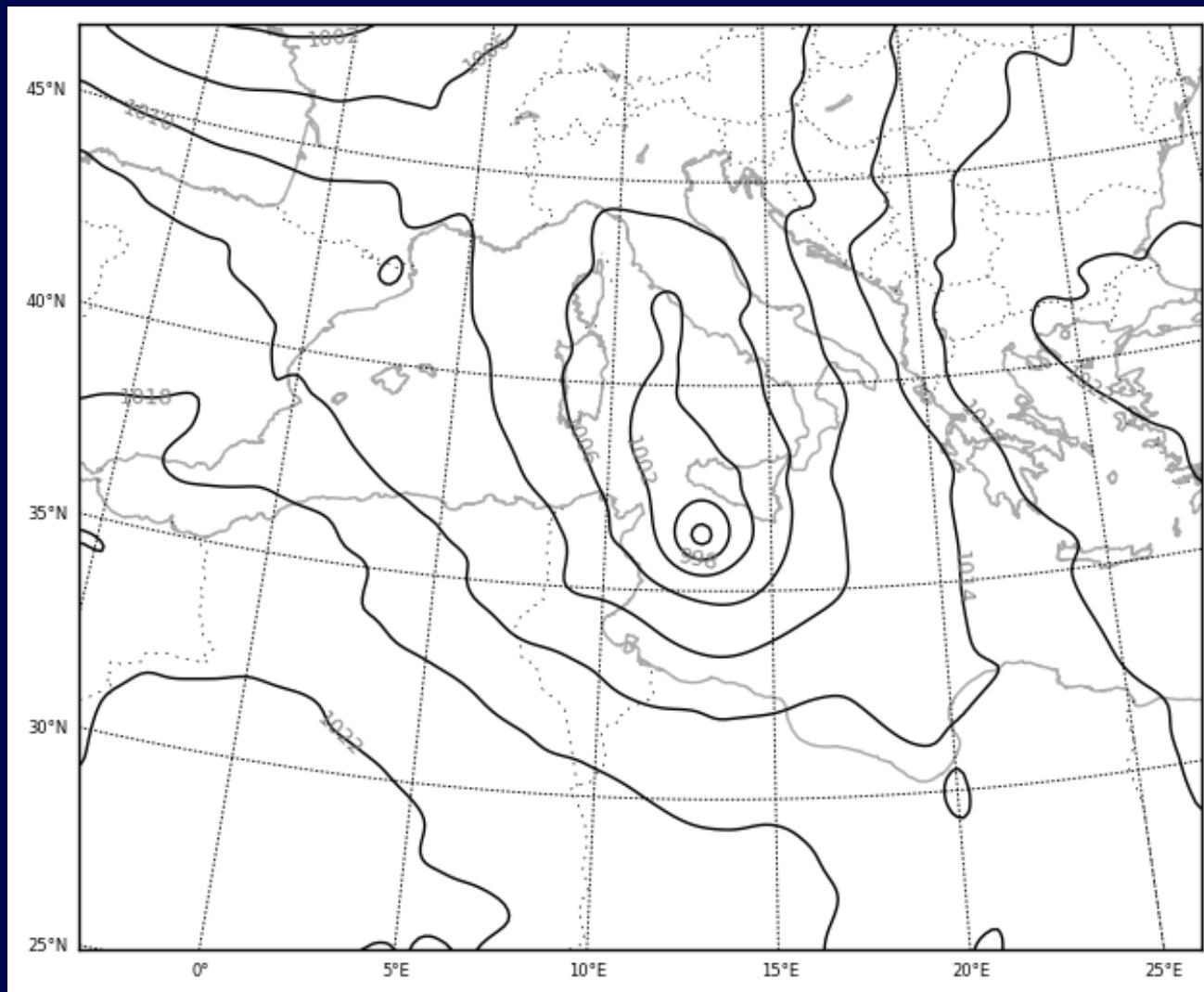
Time index: 8

# The evolution of the sea level pressure



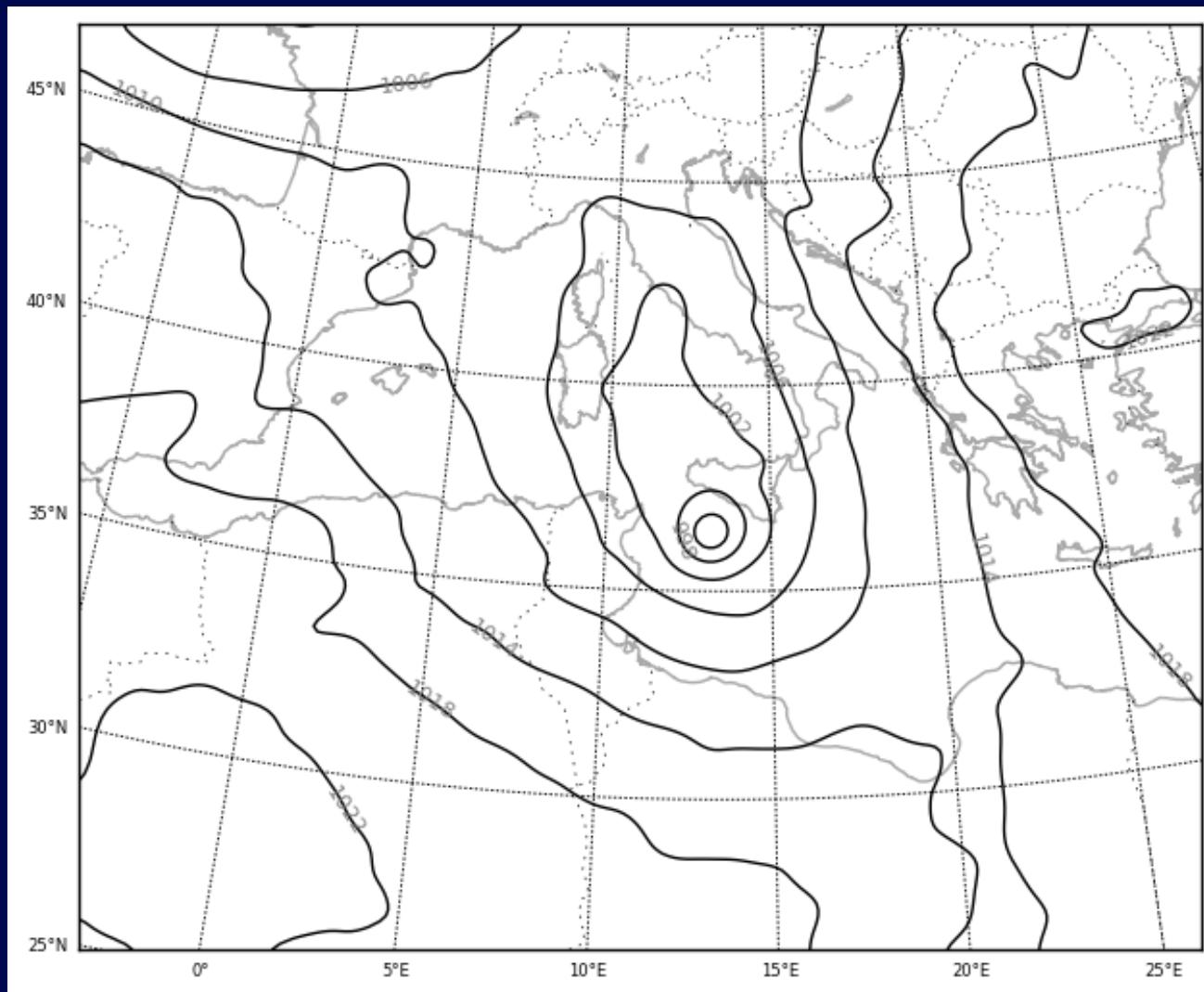
Time index: 9

# The evolution of the sea level pressure



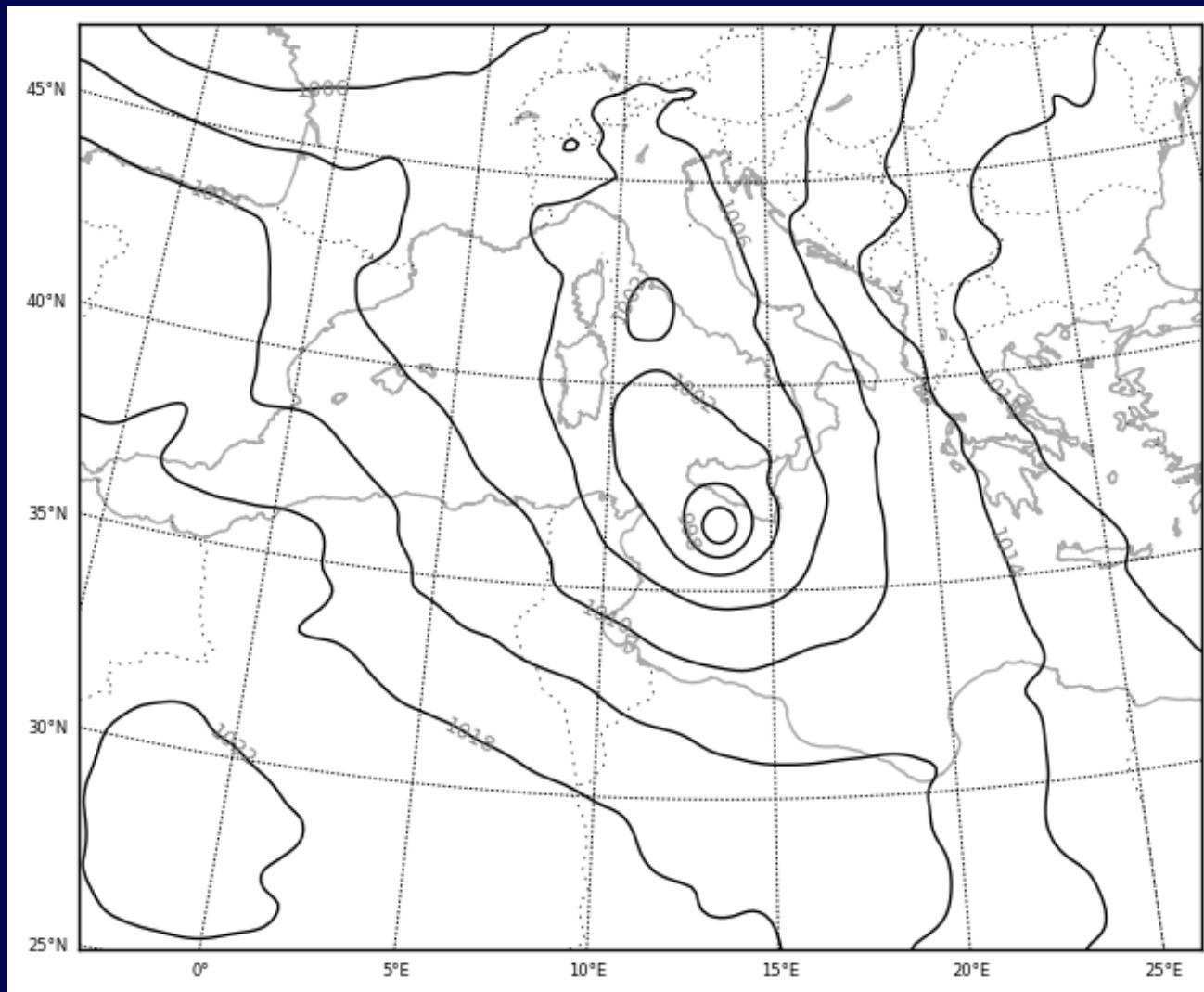
Time index: 10

# The evolution of the sea level pressure



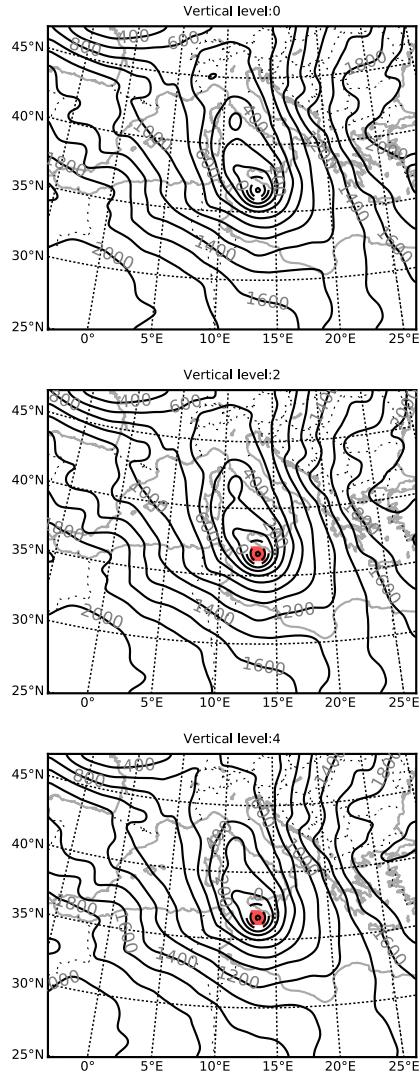
Time index: 11

# The evolution of the sea level pressure



Time index: 12

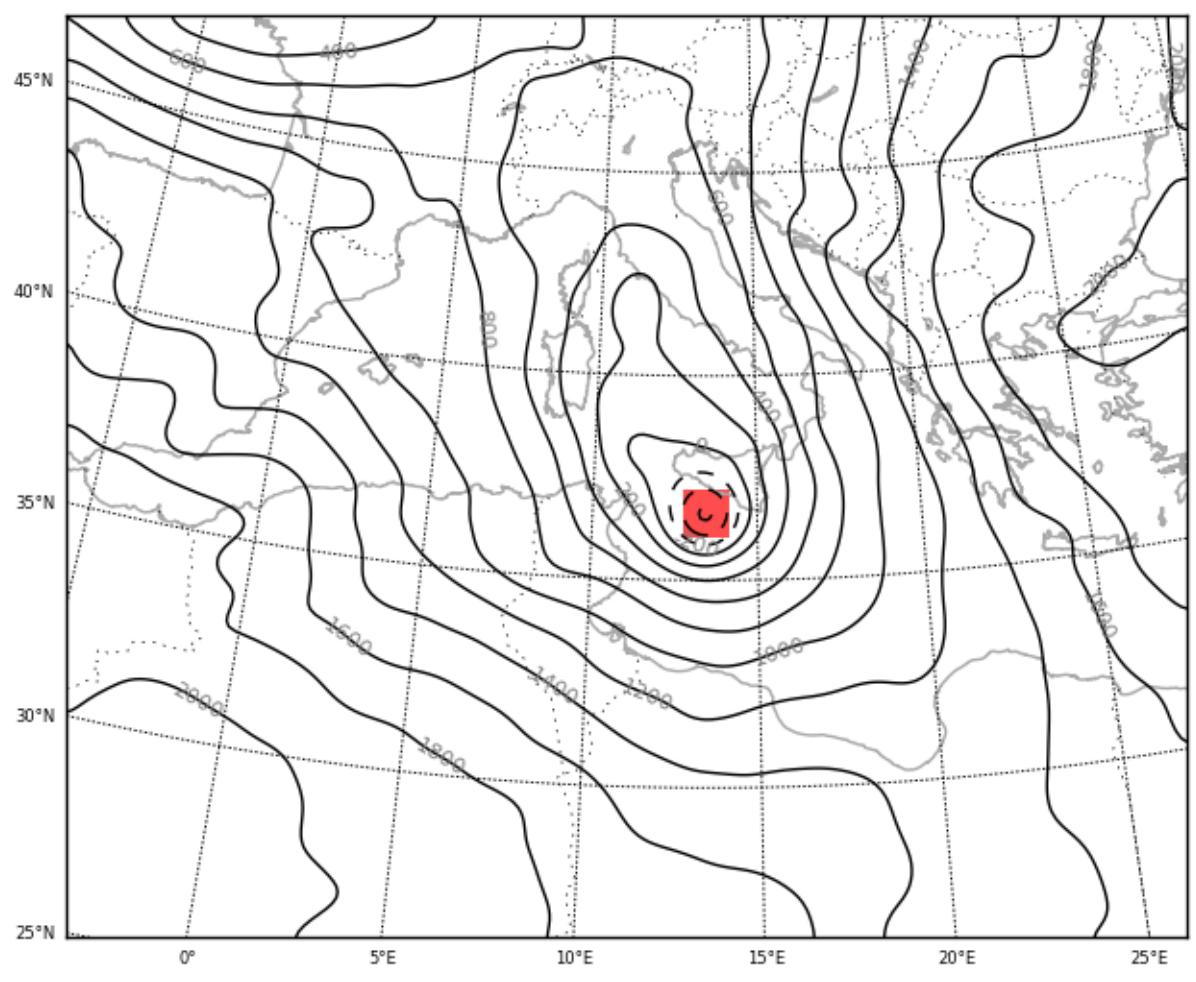
# The response functions: pressure



$$J_1 = \sum_{prism} p$$

$$\frac{\partial J_1}{\partial \vec{x}} = \begin{cases} 1, & \text{in prism for } p \\ 0, & \text{otherwise} \end{cases}$$

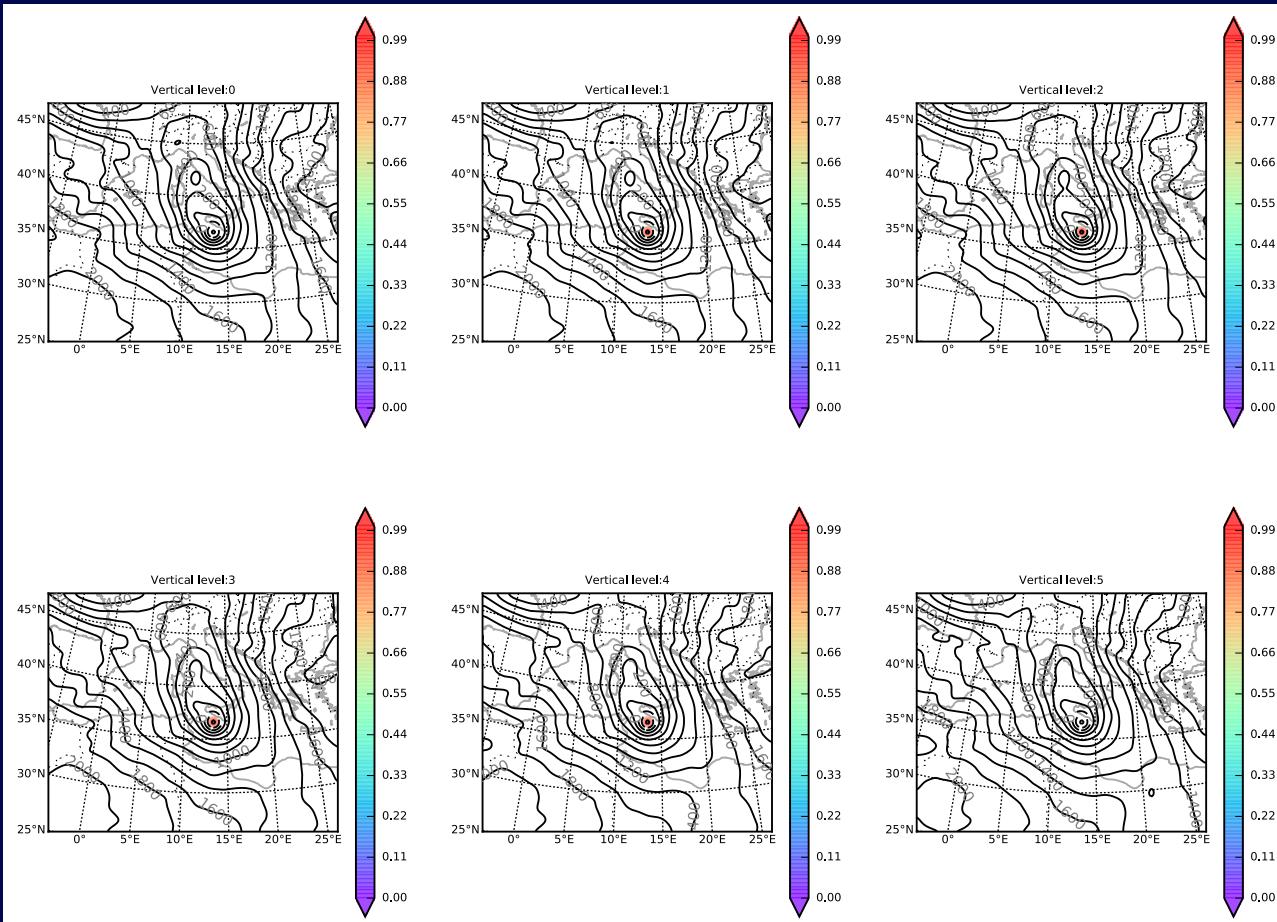
# The response functions: pressure



$$J_1 = \sum_{prism} p$$

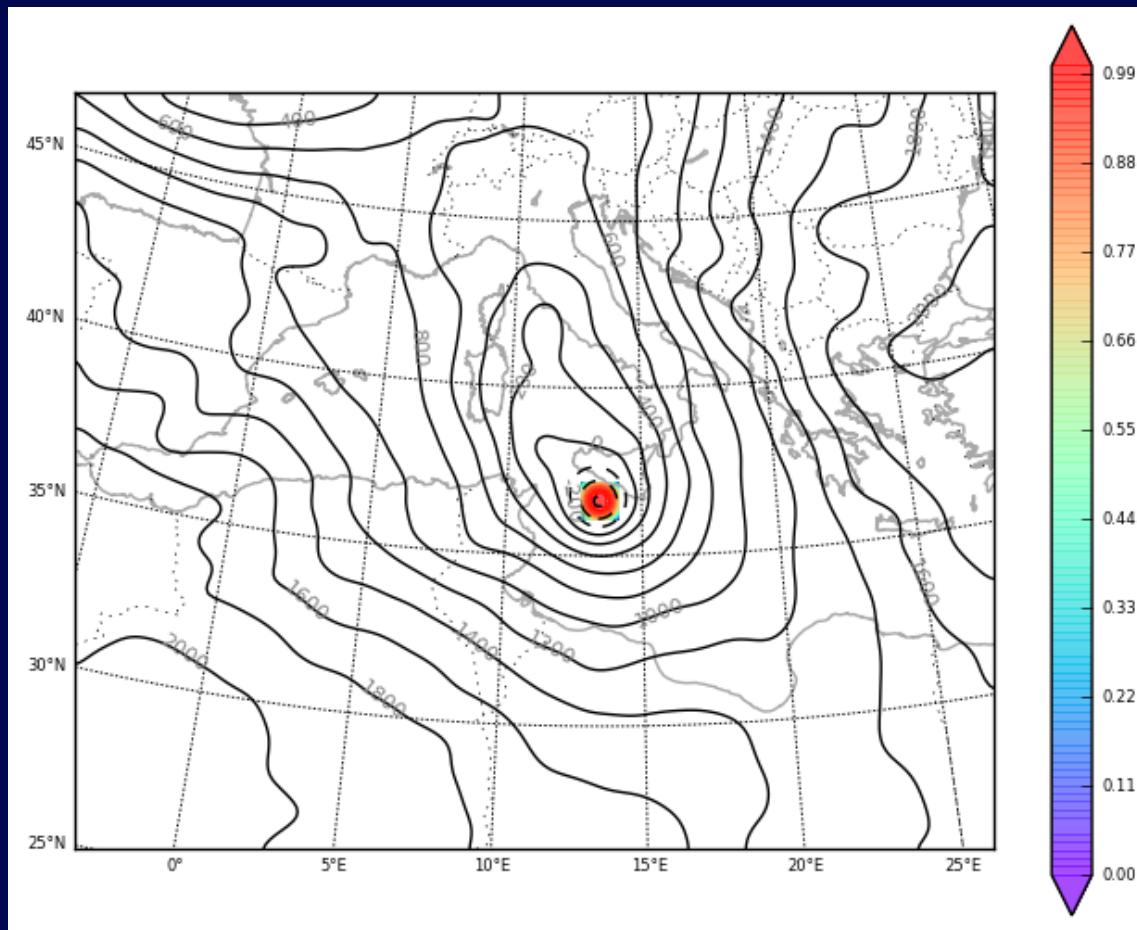
$$\frac{\partial J_1}{\partial \vec{x}} = \begin{cases} 1, & \text{in prism for } p \\ 0, & \text{otherwise} \end{cases}$$

# The response functions: cosine-modulated pressure



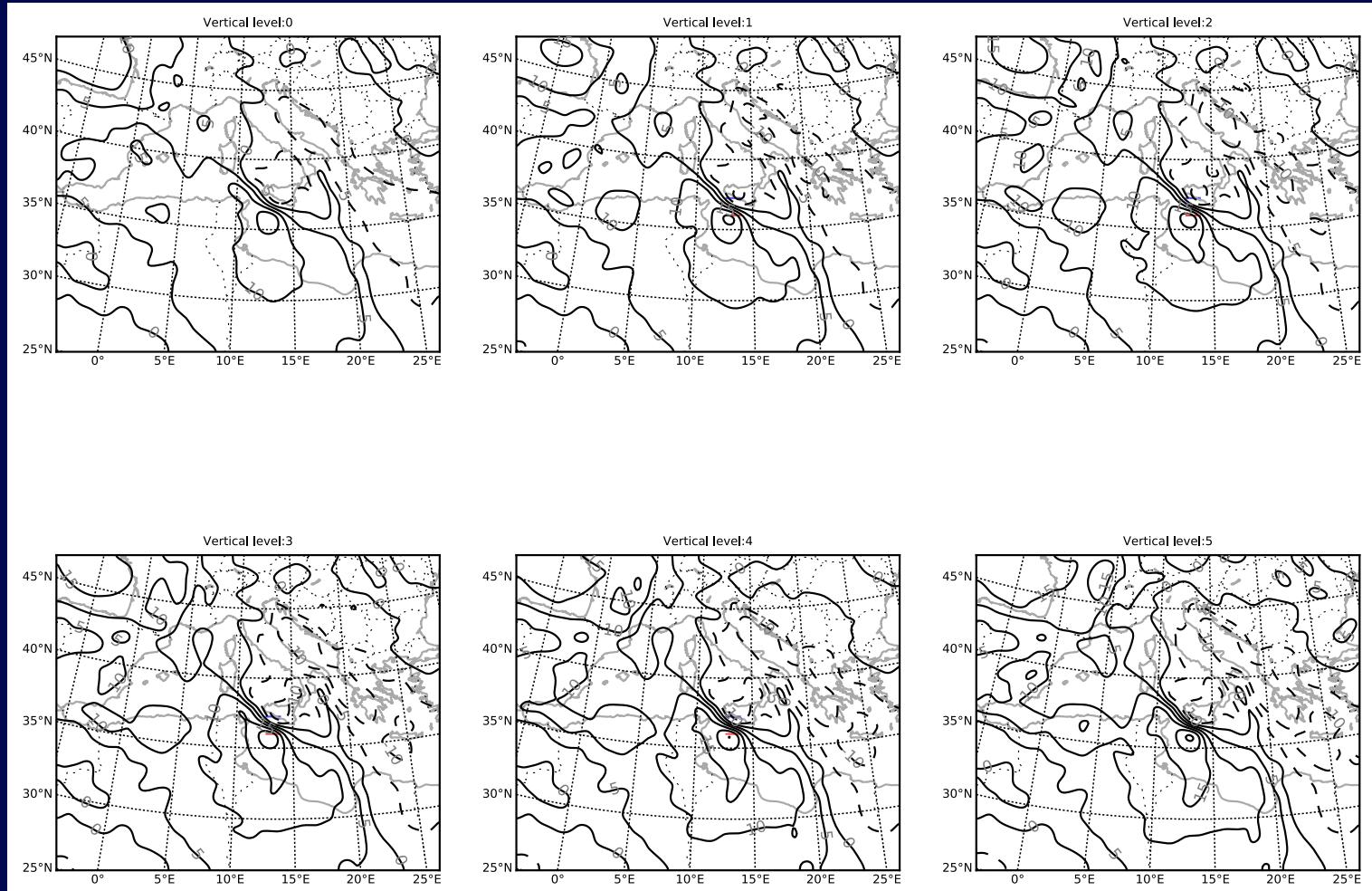
$$J_2 = \sum_{prism} \cos\left(\frac{\pi}{2d_{max}} d\right) p \quad \frac{\partial J_2}{\partial \vec{x}} = \begin{cases} \cos\left(\frac{\pi}{64} d\right), & \text{in prism for } p \\ 0, & \text{otherwise} \end{cases}$$

# The response functions: cosine-modulated pressure



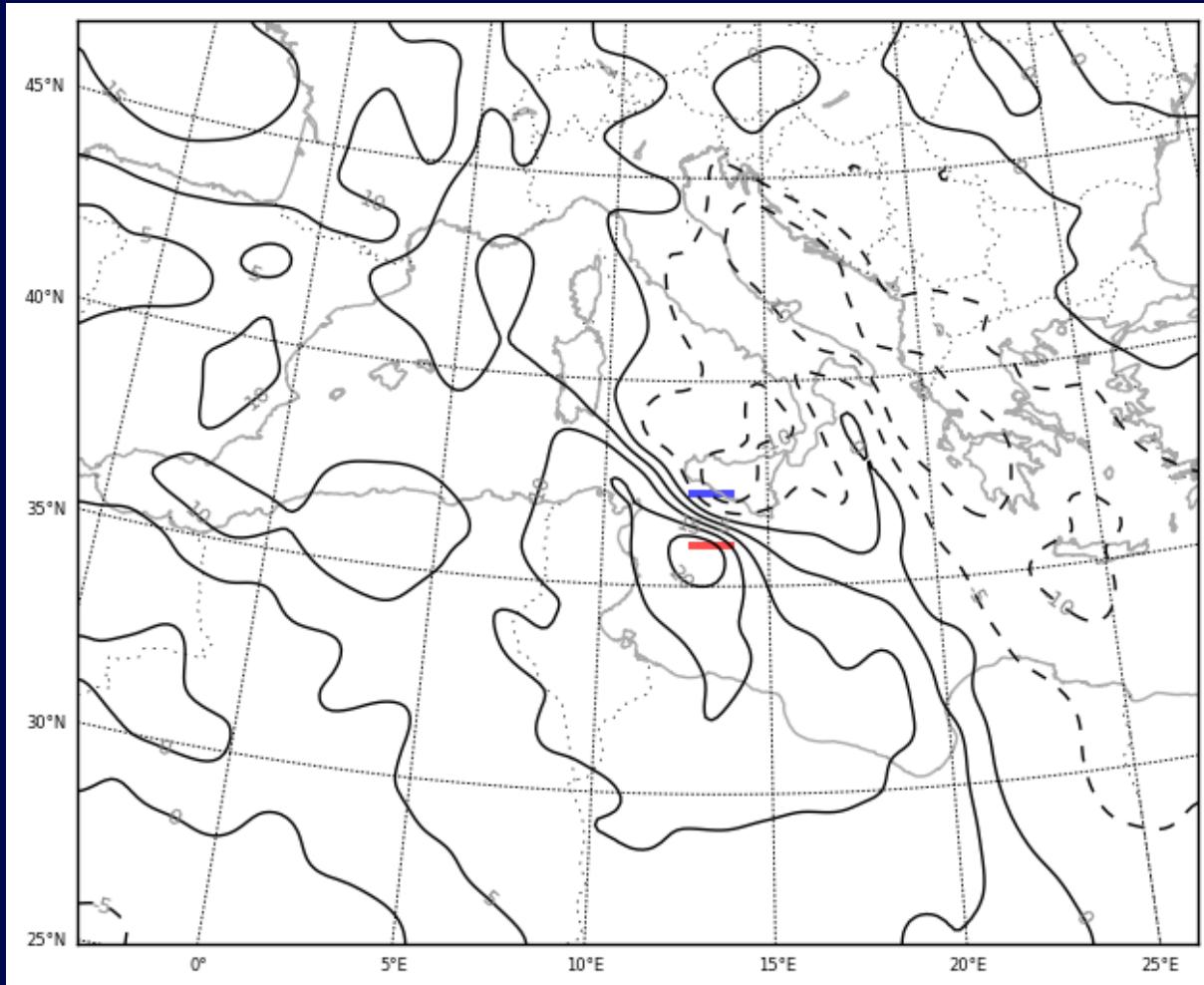
$$J_2 = \sum_{prism} \cos\left(\frac{\pi}{2d_{max}} d\right) p \quad \frac{\partial J_2}{\partial \vec{x}} = \begin{cases} \cos\left(\frac{\pi}{64}d\right), & \text{in prism for } p \\ 0, & \text{otherwise} \end{cases}$$

# The response functions: relative vorticity



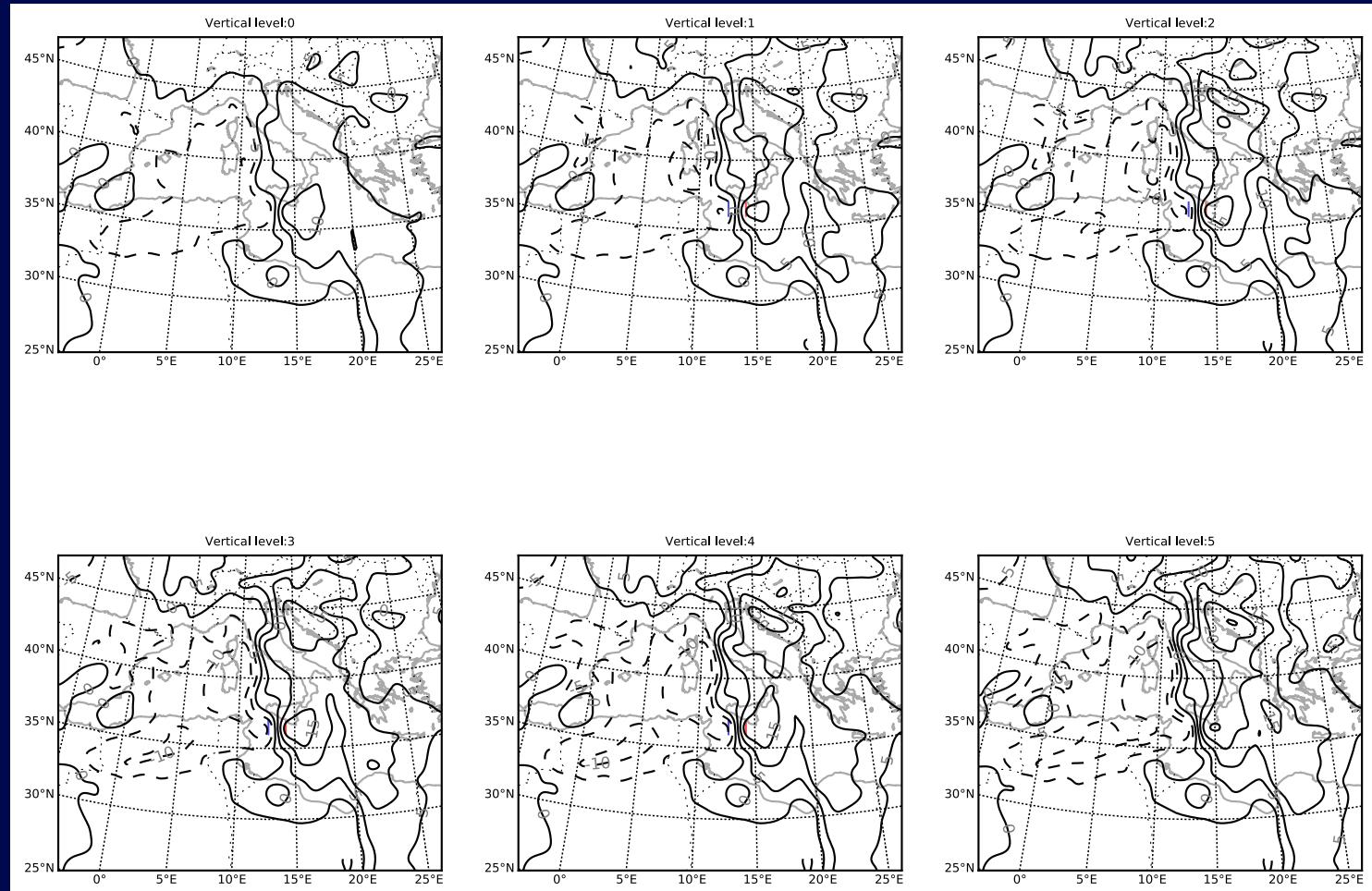
$$J_3 = \sum_{prism} \zeta \quad \frac{\partial J_3}{\partial \vec{u}} = \begin{cases} 1/2\Delta, & \text{if } ist + 1, jst, kst \leq i, j, k \leq iend + 1, jend, kend \\ -1/2\Delta, & \text{if } ist - 1, jst, kst \leq i, j, k \leq iend - 1, jend, kend \\ 0, & \text{otherwise} \end{cases}$$

# The response functions: relative vorticity



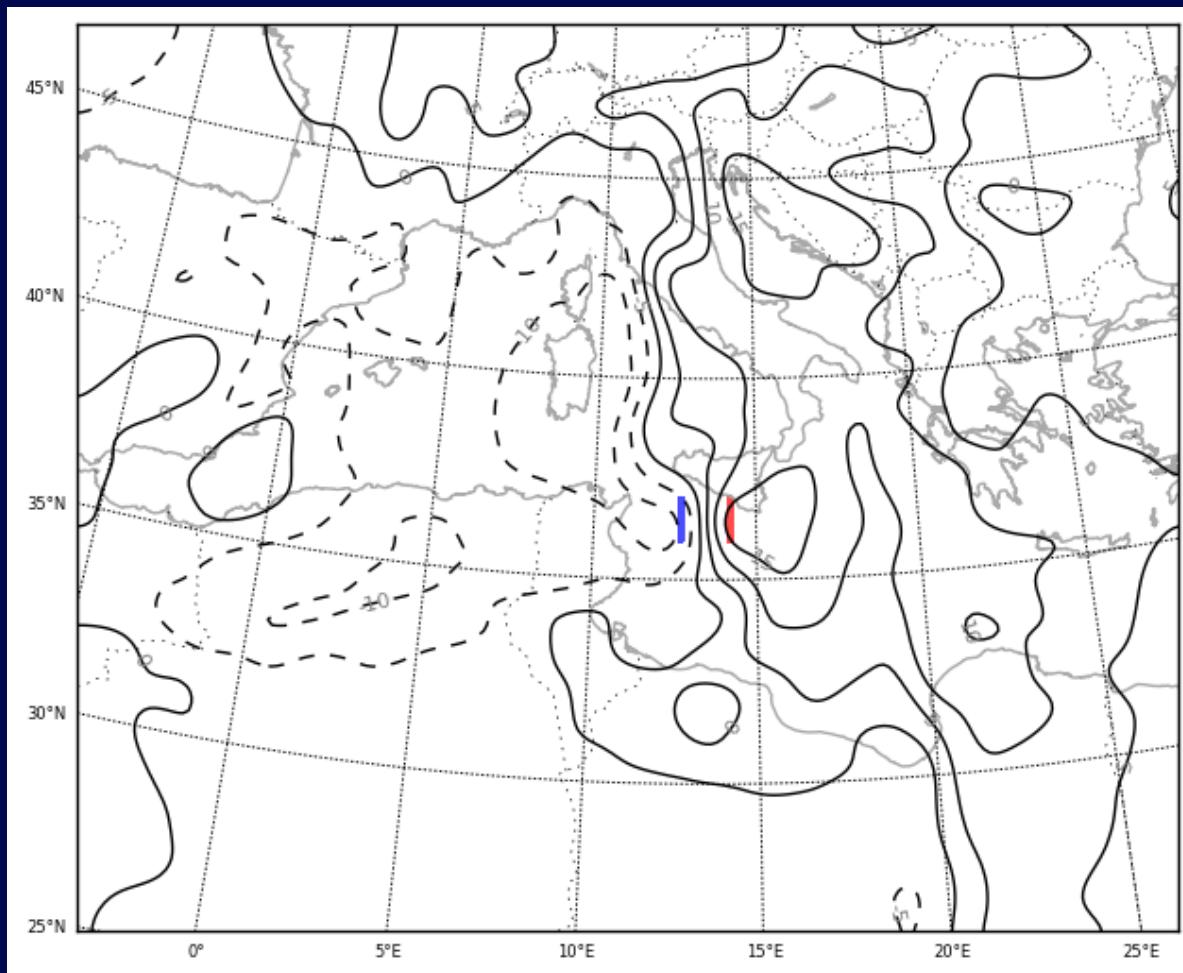
$$J_3 = \sum_{prism} \zeta \quad \frac{\partial J_3}{\partial \vec{u}} = \begin{cases} 1/2\Delta, & \text{if } ist + 1, jst, kst \leq i, j, k \leq iend + 1, jend, kend \\ -1/2\Delta, & \text{if } ist - 1, jst, kst \leq i, j, k \leq iend - 1, jend, kend \\ 0, & \text{otherwise} \end{cases}$$

# The response functions: relative vorticity



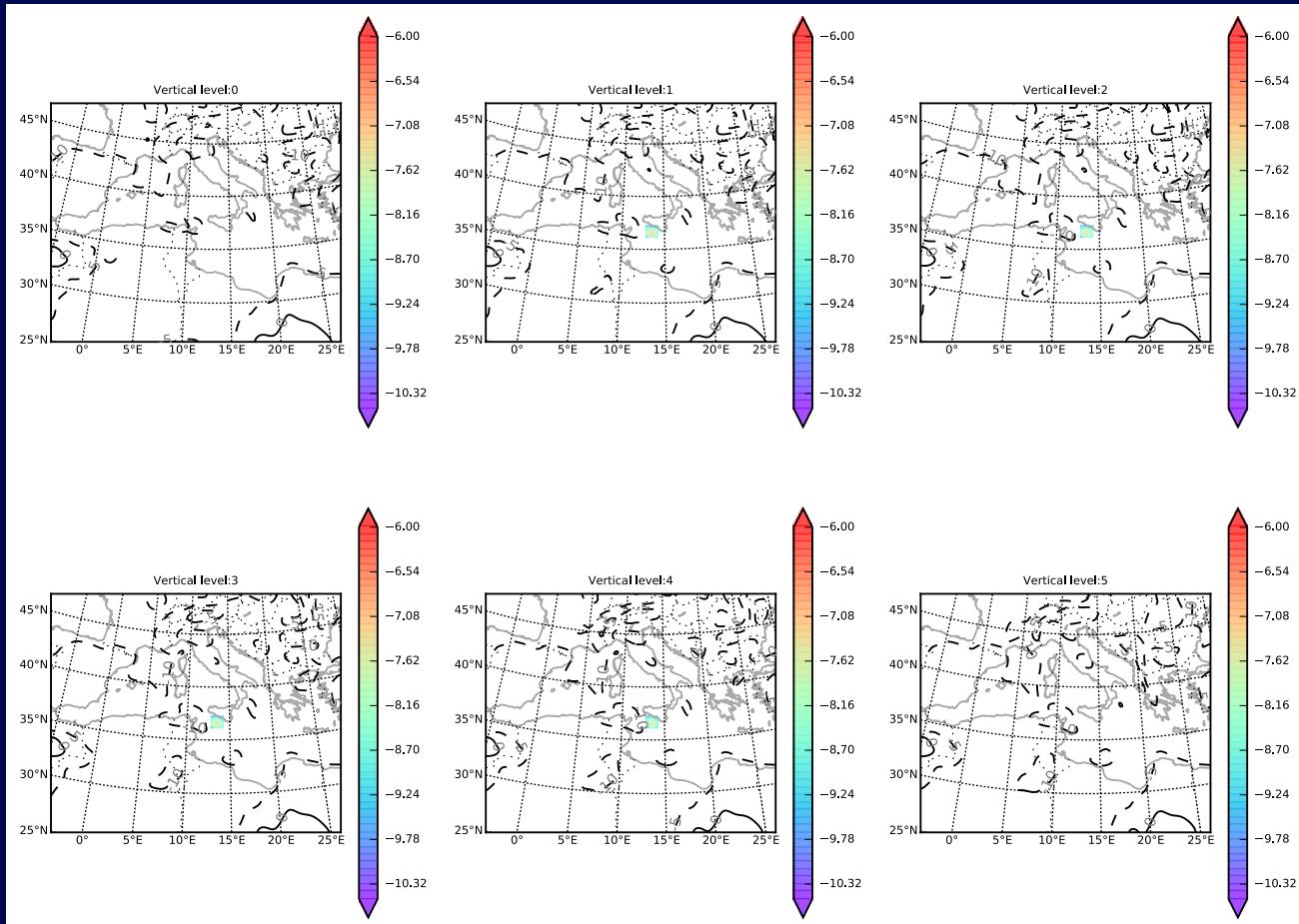
$$J_3 = \sum_{prism} \zeta \quad \frac{\partial J_3}{\partial \vec{v}} = \begin{cases} 1/2\Delta, & \text{if } ist + 1, jst, kst \leq i, j, k \leq iend + 1, jend, kend \\ -1/2\Delta, & \text{if } ist - 1, jst, kst \leq i, j, k \leq iend - 1, jend, kend \\ 0, & \text{otherwise} \end{cases}$$

# The response functions: relative vorticity



$$J_3 = \sum_{prism} \zeta \quad \frac{\partial J_3}{\partial \vec{v}} = \begin{cases} 1/2\Delta, & \text{if } ist + 1, jst, kst \leq i, j, k \leq iend + 1, jend, kend \\ -1/2\Delta, & \text{if } ist - 1, jst, kst \leq i, j, k \leq iend - 1, jend, kend \\ 0, & \text{otherwise} \end{cases}$$

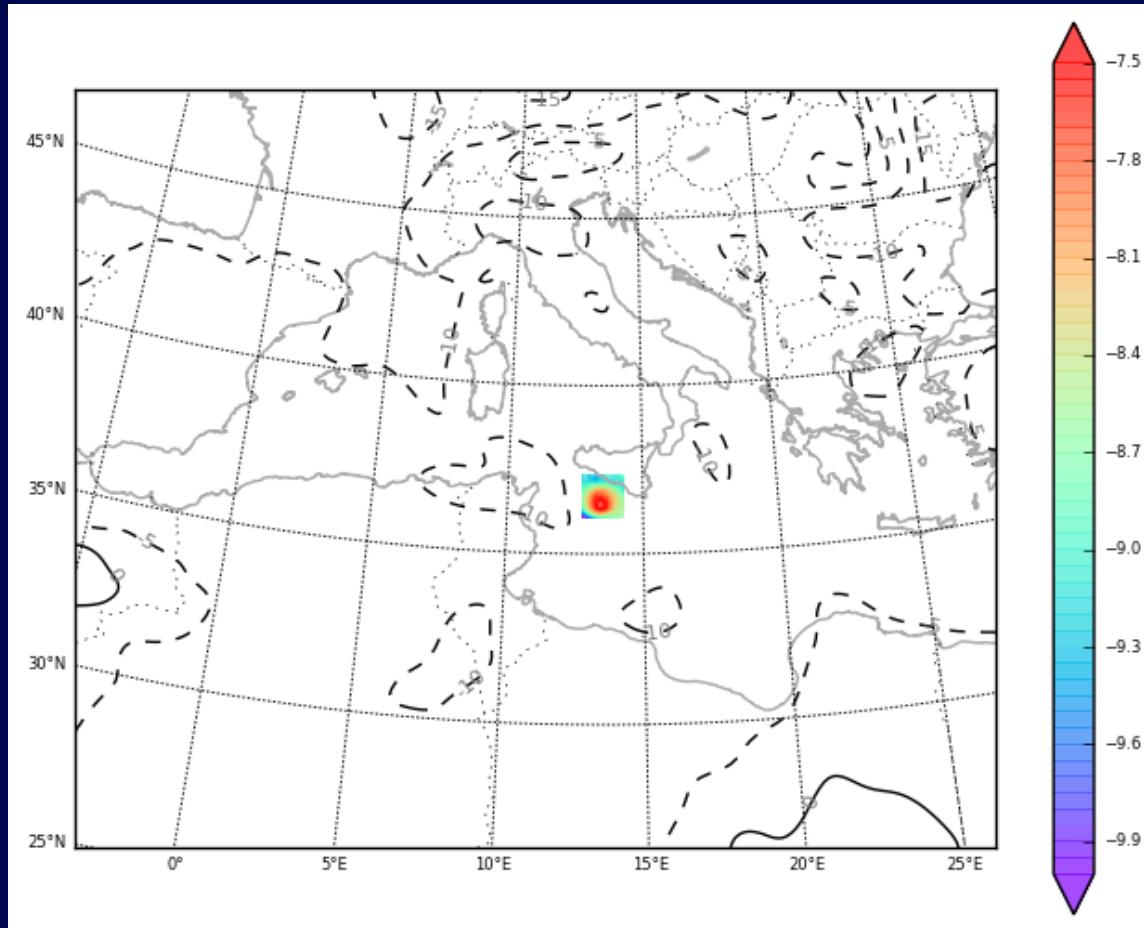
# The response functions: weighted dry total energy



$$J_4 = \frac{1}{2} \sum_{prism} T^2 + u^2 + v^2$$

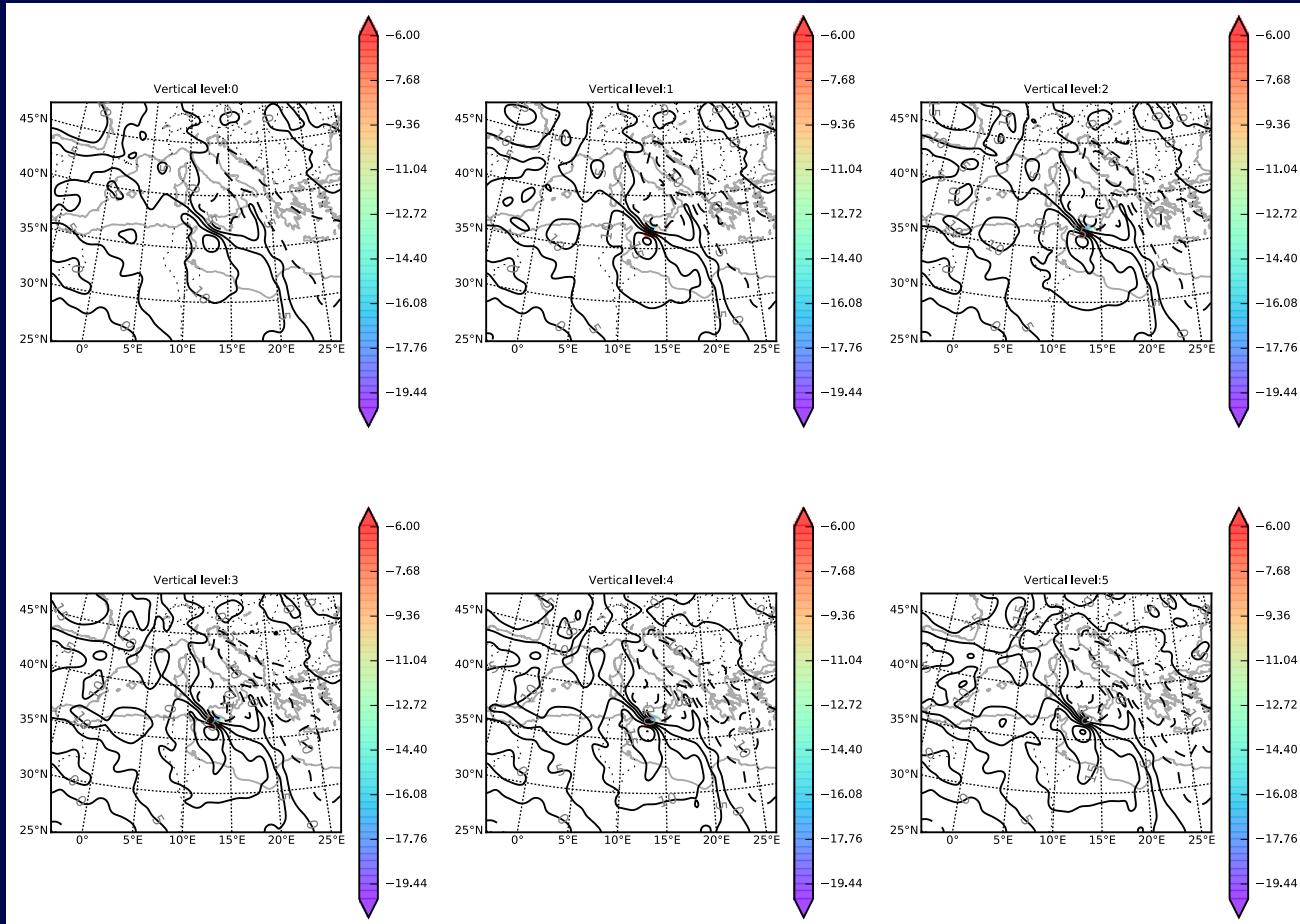
$$\frac{\partial J_4}{\partial \vec{T}} = \begin{cases} T, & \text{in prism} \\ 0, & \text{otherwise} \end{cases}$$

# The response functions: weighted dry total energy



$$J_4 = \frac{1}{2} \sum_{prism} T^2 + u^2 + v^2 \quad \frac{\partial J_4}{\partial \vec{T}} = \begin{cases} T, & \text{in prism} \\ 0, & \text{otherwise} \end{cases}$$

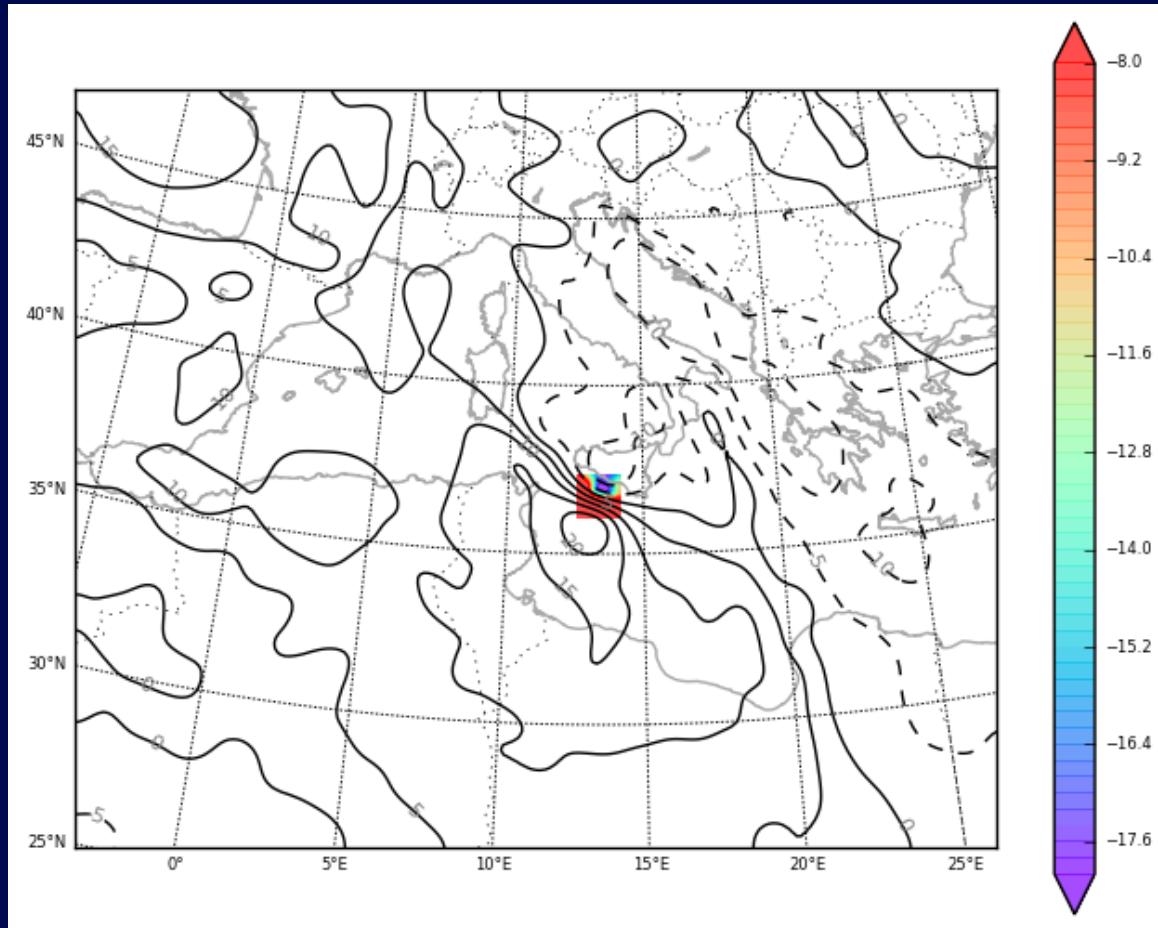
# The response functions: weighted dry total energy



$$J_4 = \frac{1}{2} \sum_{prism} T^2 + u^2 + v^2$$

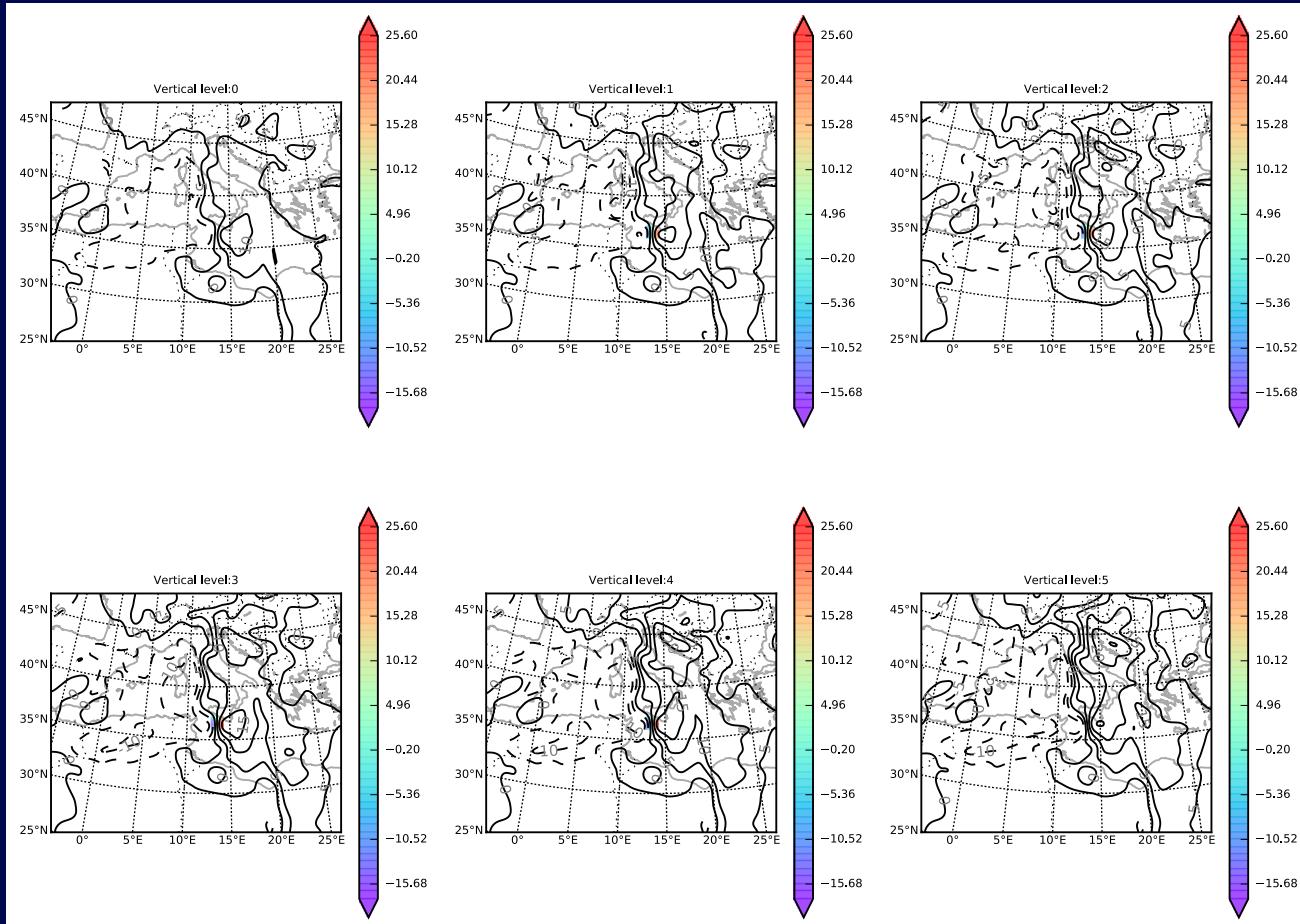
$$\frac{\partial J_4}{\partial \vec{u}} = \begin{cases} u, & \text{in prism} \\ 0, & \text{otherwise} \end{cases}$$

# The response functions: weighted dry total energy



$$J_4 = \frac{1}{2} \sum_{prism} T^2 + u^2 + v^2 \quad \frac{\partial J_4}{\partial \vec{u}} = \begin{cases} u, & \text{in prism} \\ 0, & \text{otherwise} \end{cases}$$

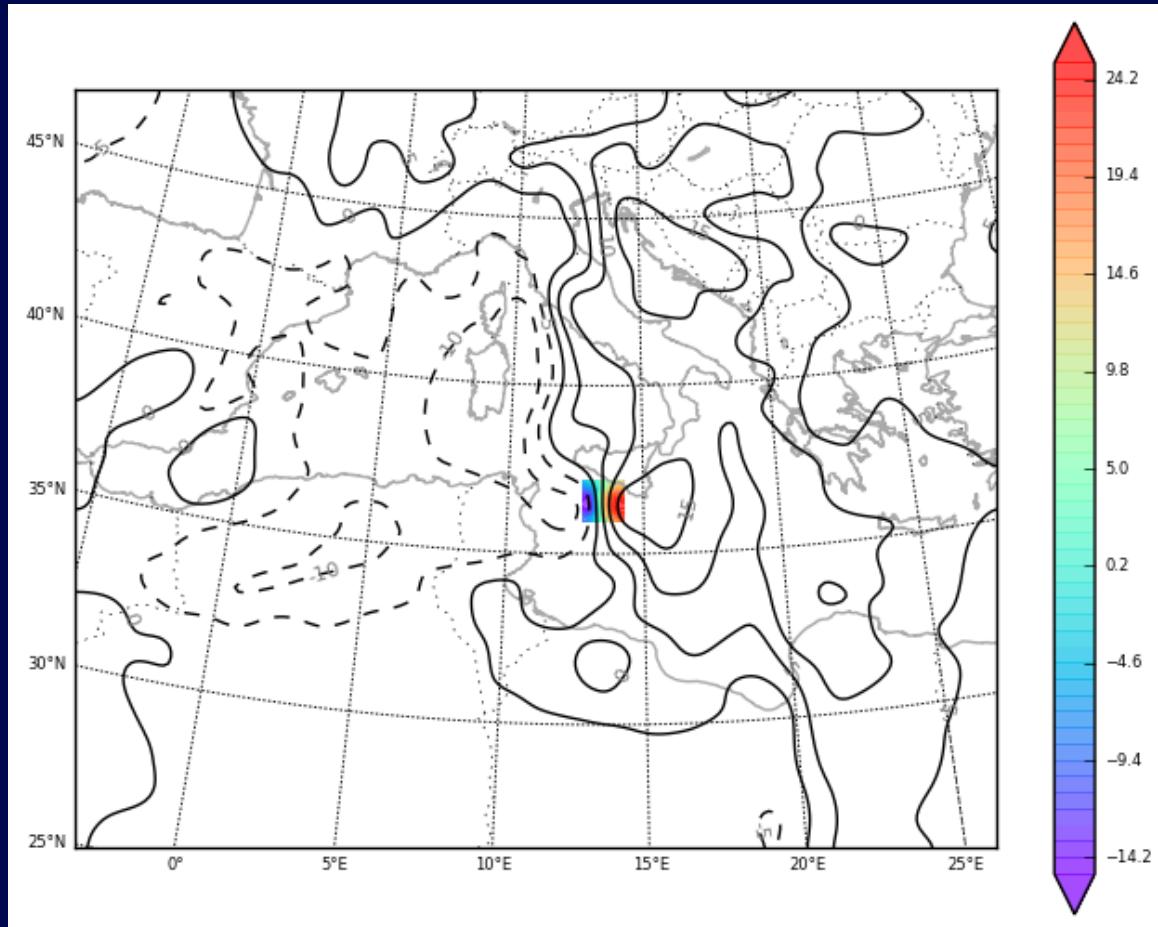
# The response functions: weighted dry total energy



$$J_4 = \frac{1}{2} \sum_{prism} T^2 + u^2 + v^2$$

$$\frac{\partial J_4}{\partial \vec{v}} = \begin{cases} v, & \text{in prism} \\ 0, & \text{otherwise} \end{cases}$$

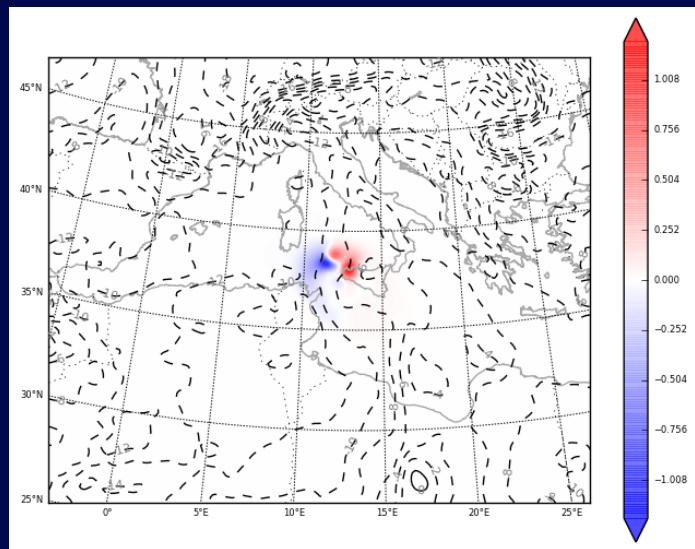
# The response functions: weighted dry total energy



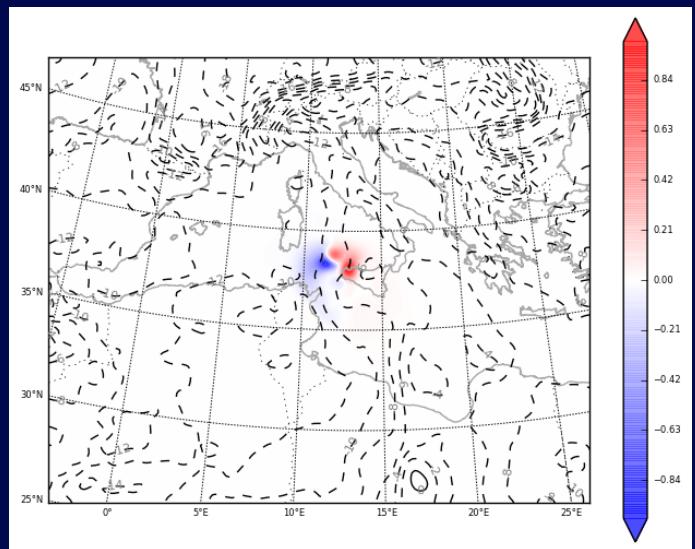
$$J_4 = \frac{1}{2} \sum_{prism} T^2 + u^2 + v^2 \quad \frac{\partial J_4}{\partial \vec{v}} = \begin{cases} v, & \text{in prism} \\ 0, & \text{otherwise} \end{cases}$$

# Adjoint sensitivities to temperature for cold start

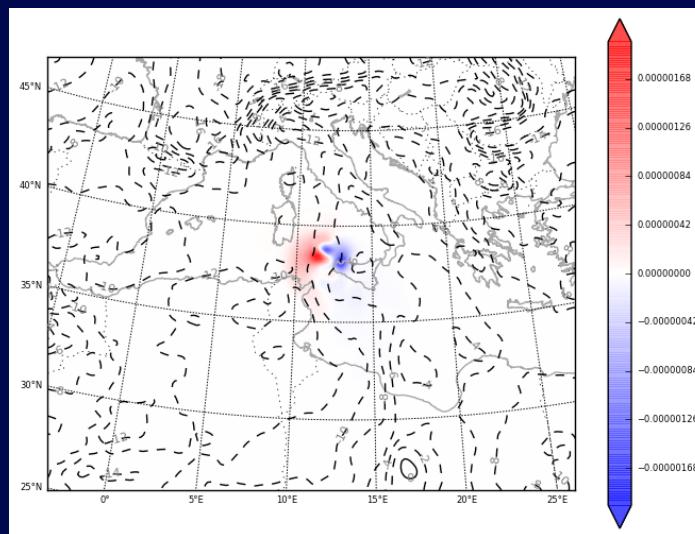
p



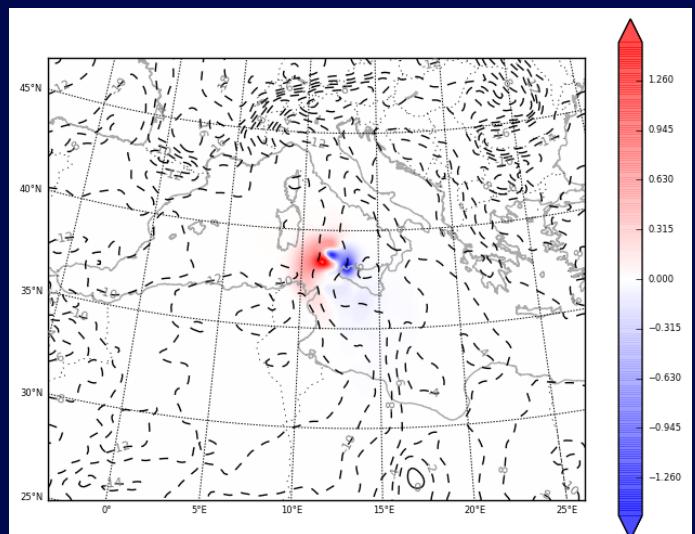
cos p



vort

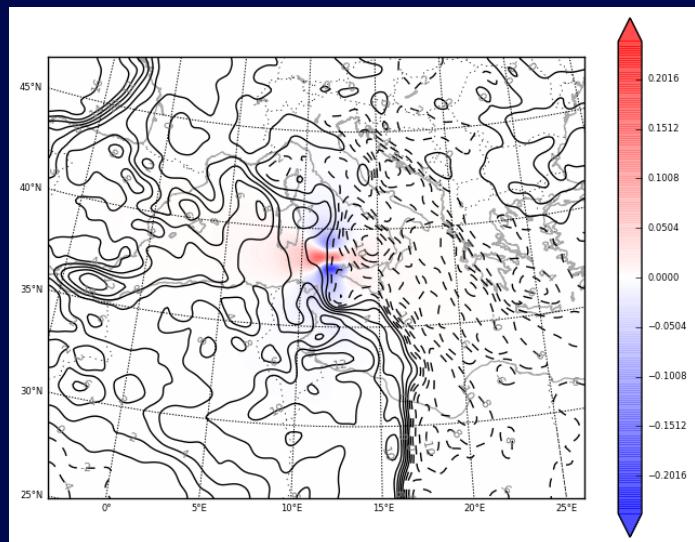


dryen

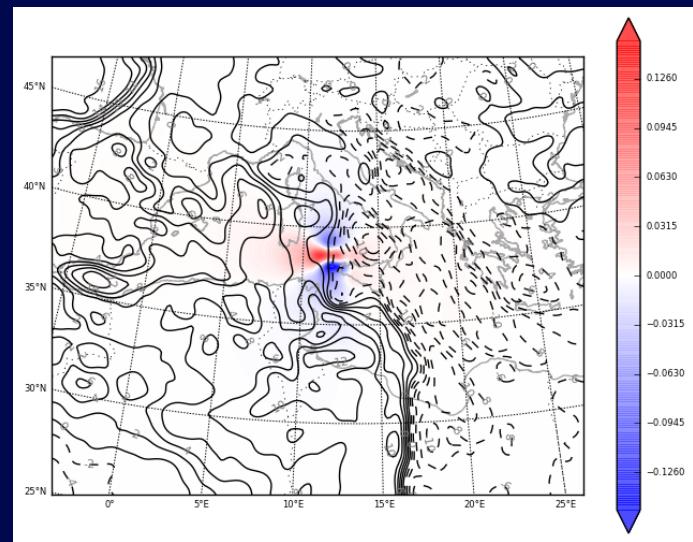
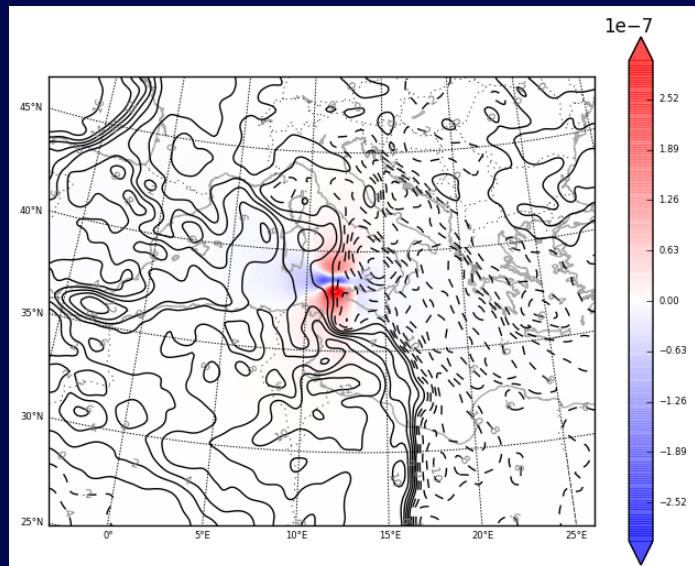


# Adjoint sensitivities to u wind for cold start

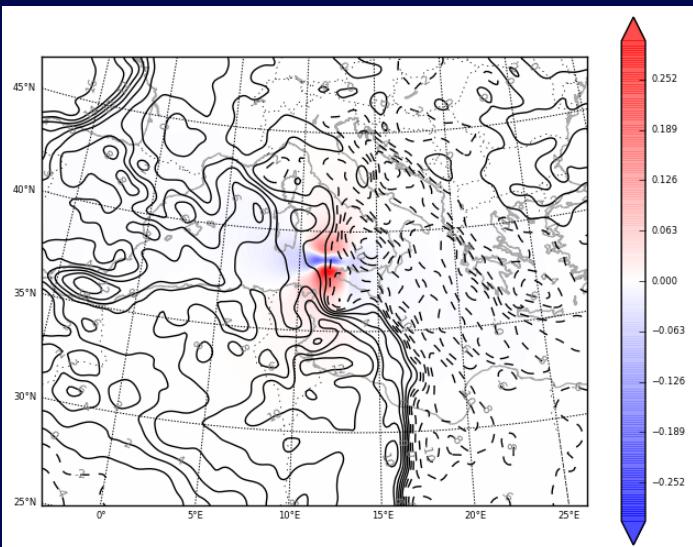
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vort



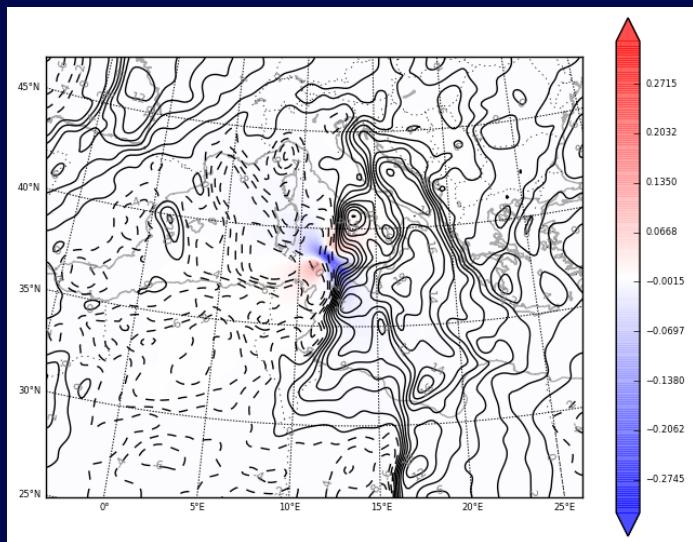
$\cos p$



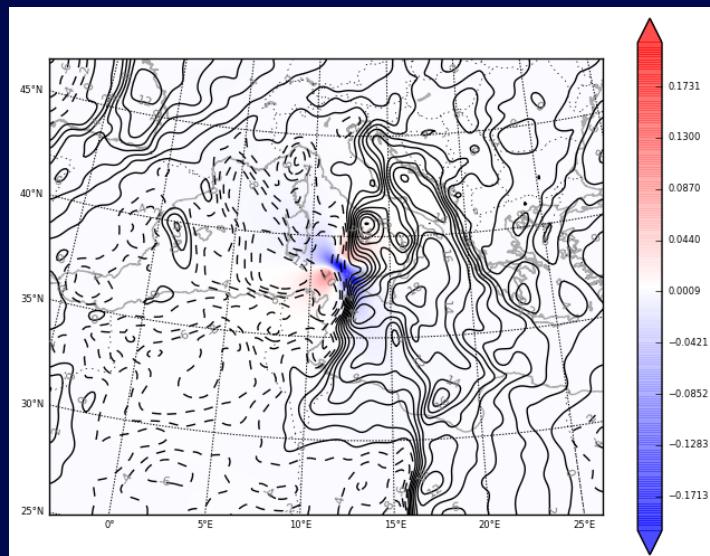
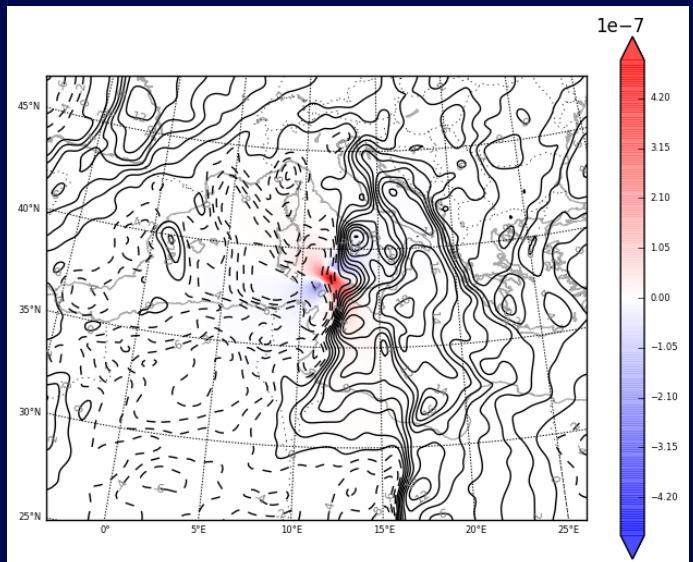
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# Adjoint sensitivities to v wind for cold start

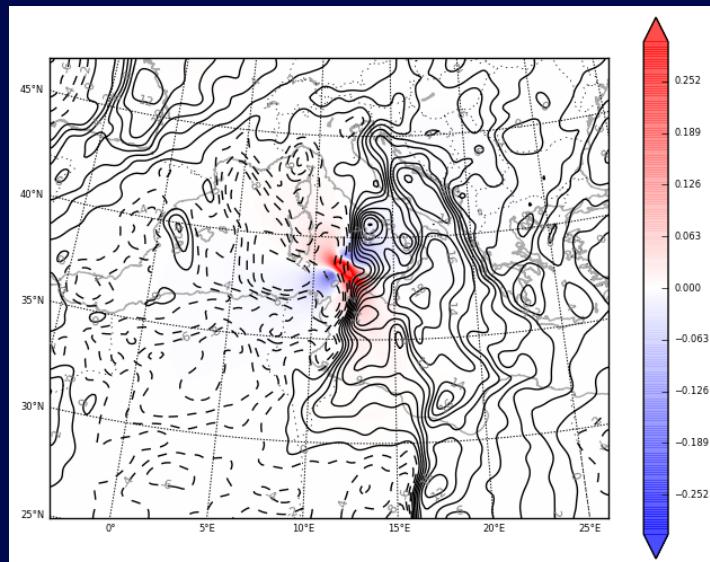
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vort

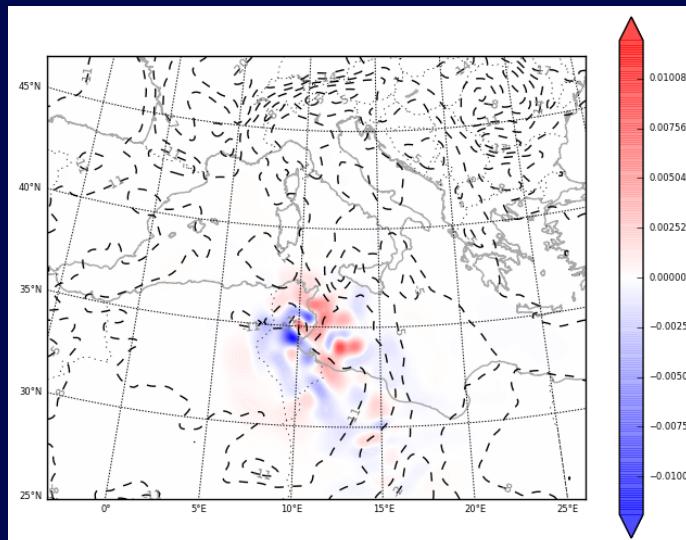
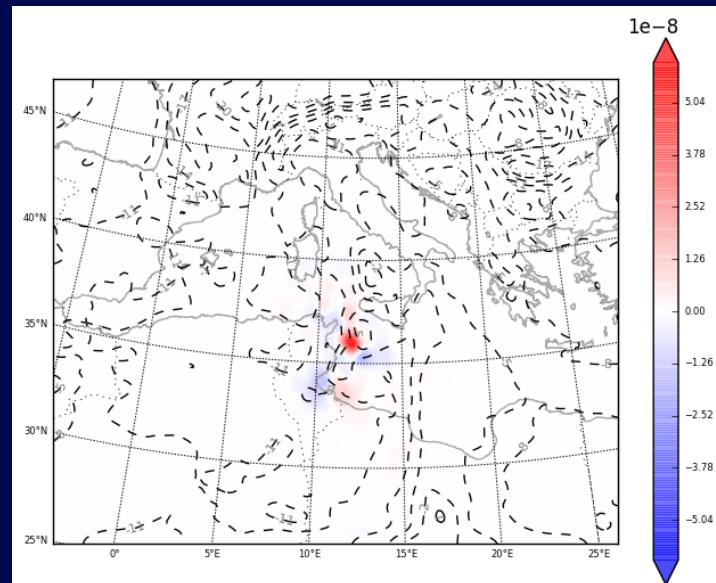
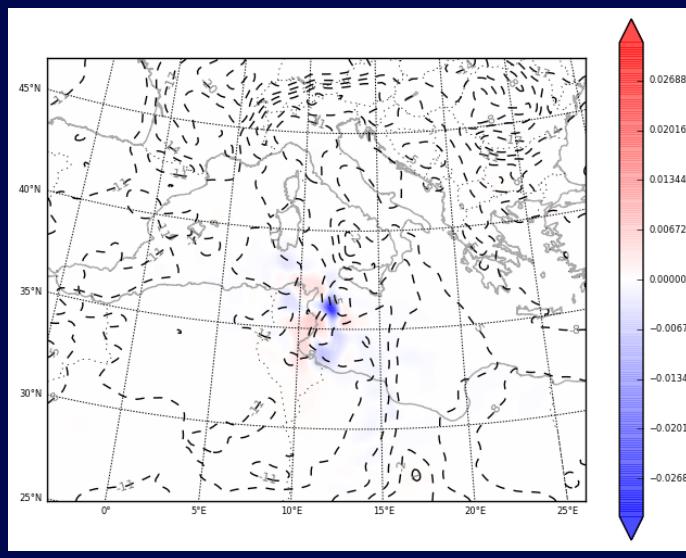
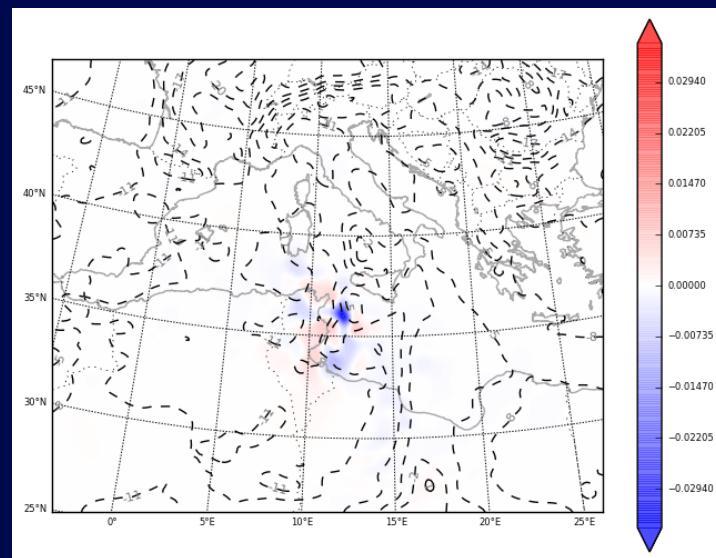


$\cos p$

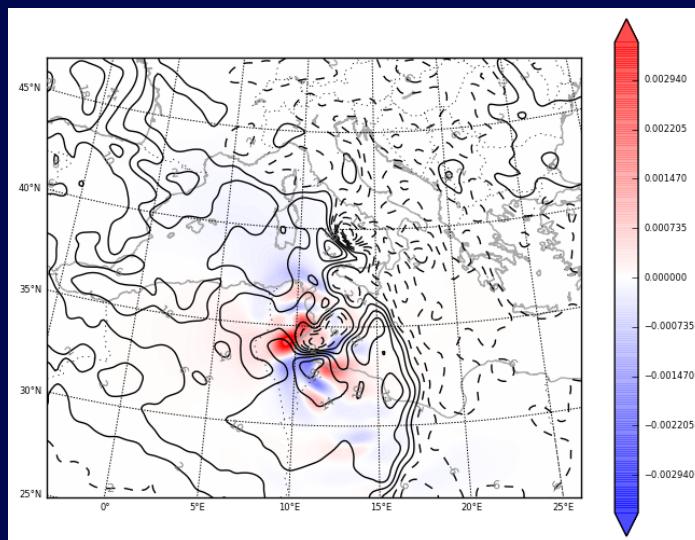
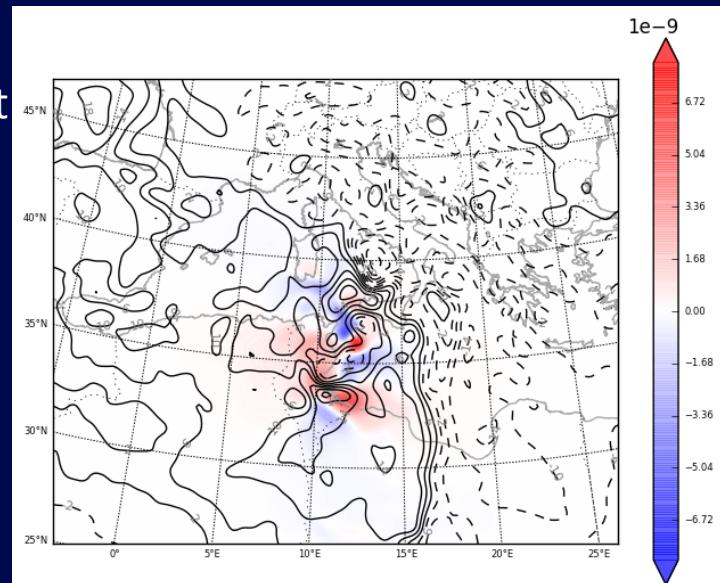
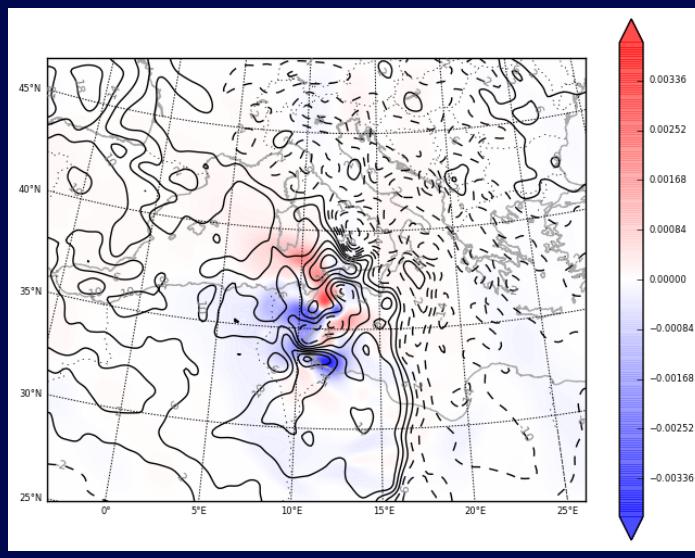
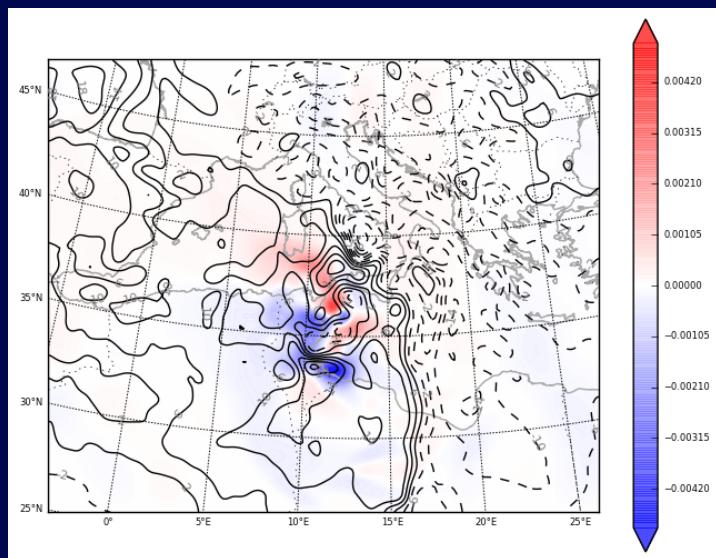


dryen

# Adjoint sensitivities to temperature for warm start

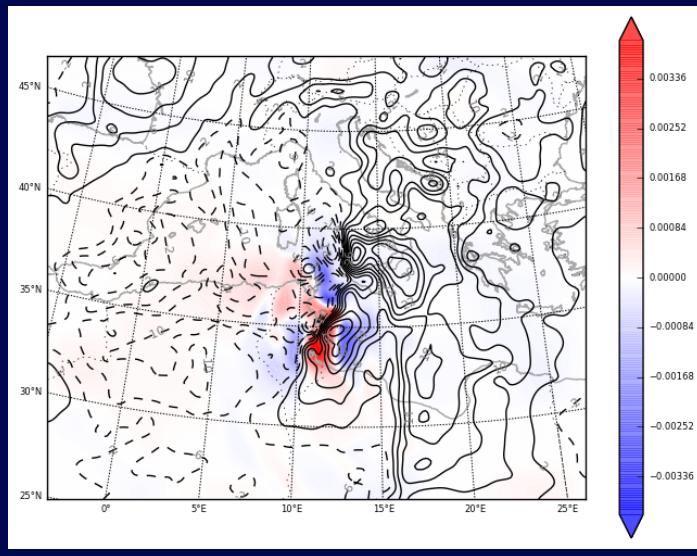
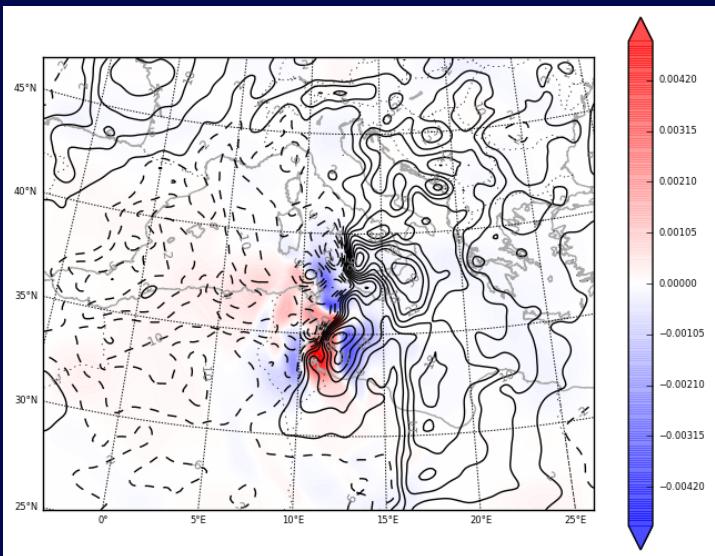


# Adjoint sensitivities to u wind for warm start

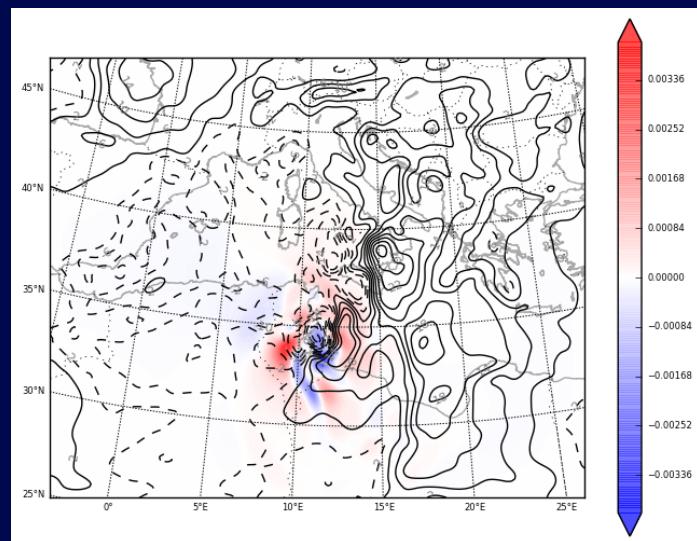
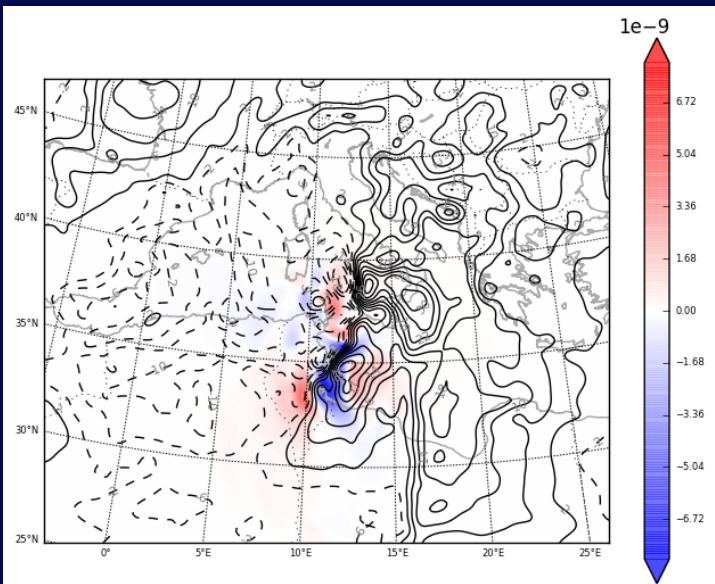


# Adjoint sensitivities to v wind for warm start

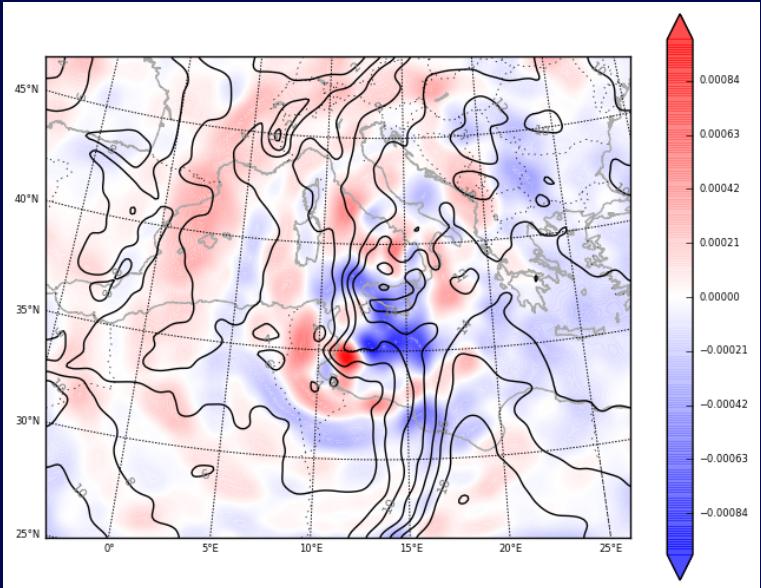
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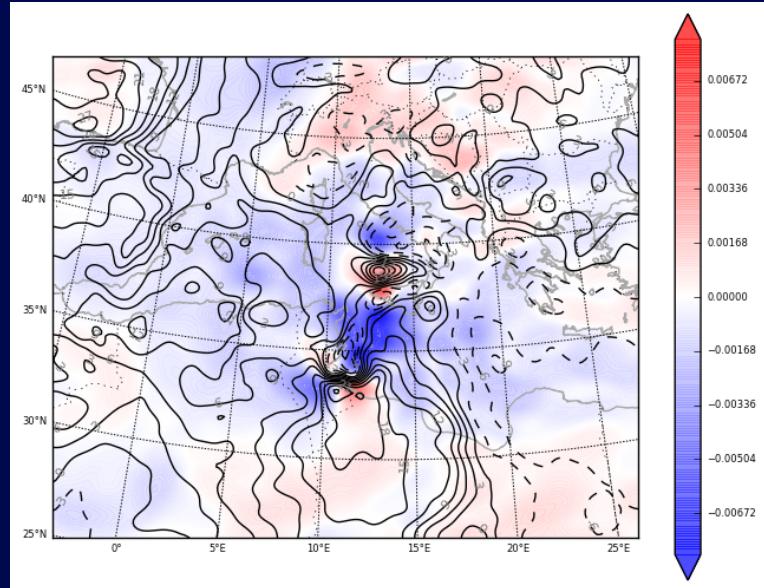
vort



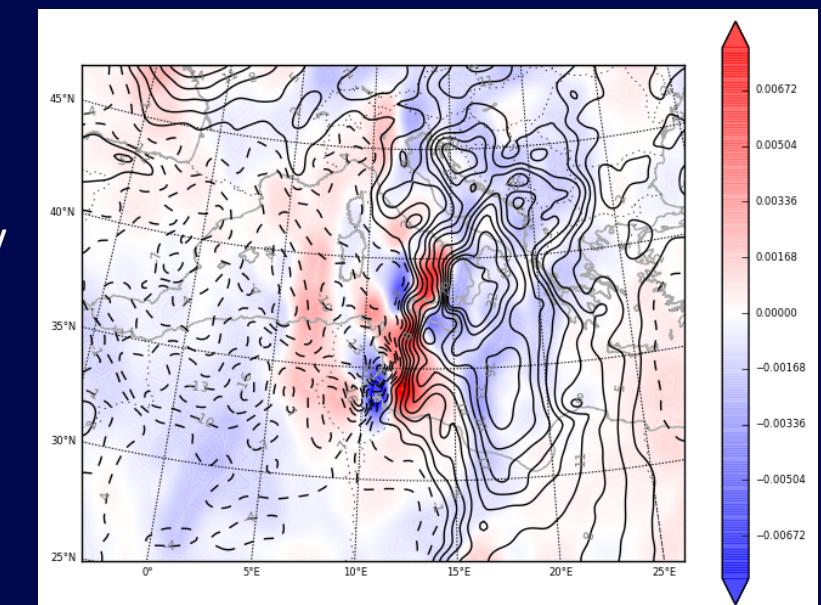
# Ensemble sensitivities



$T$

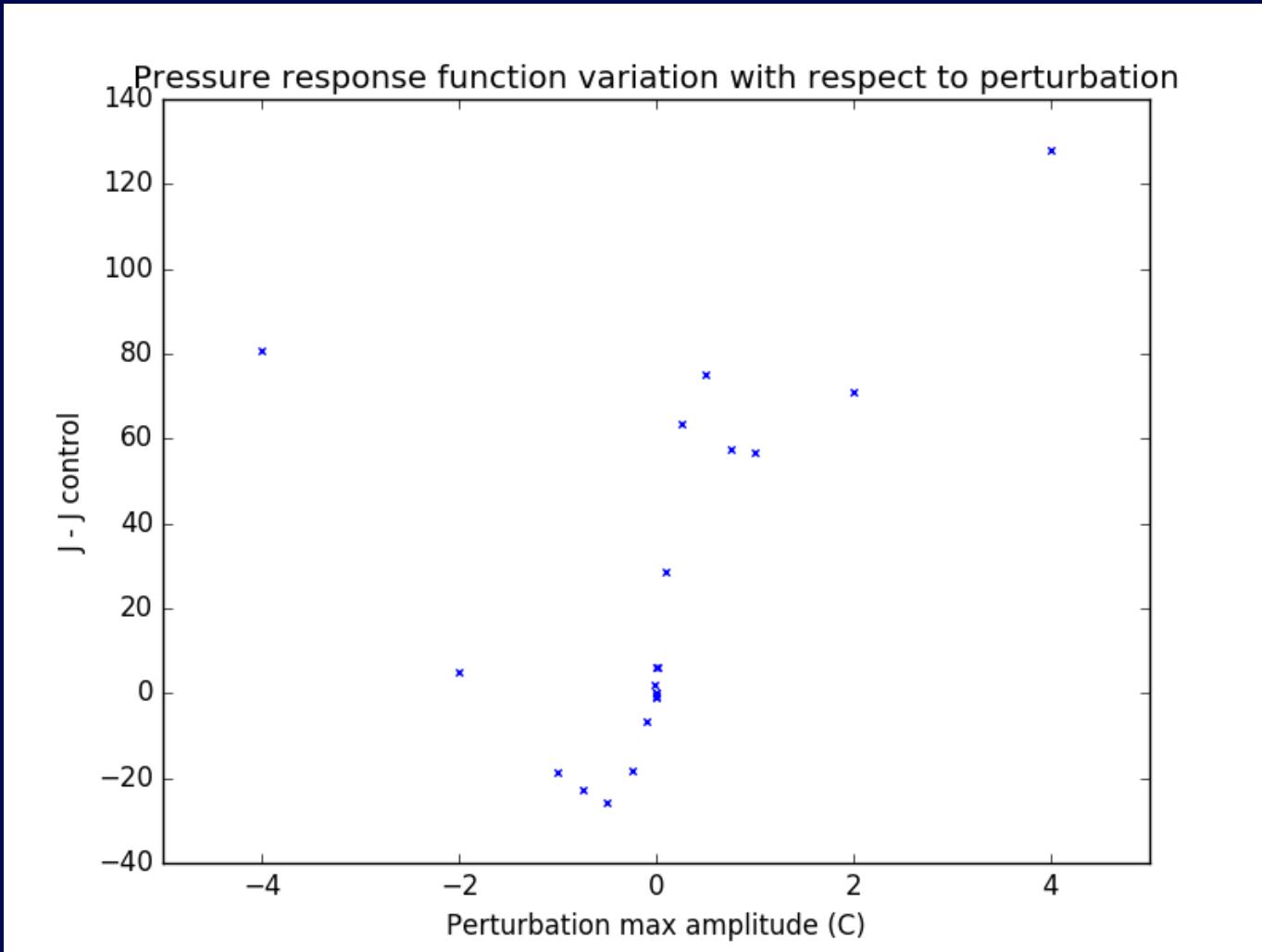


$u$

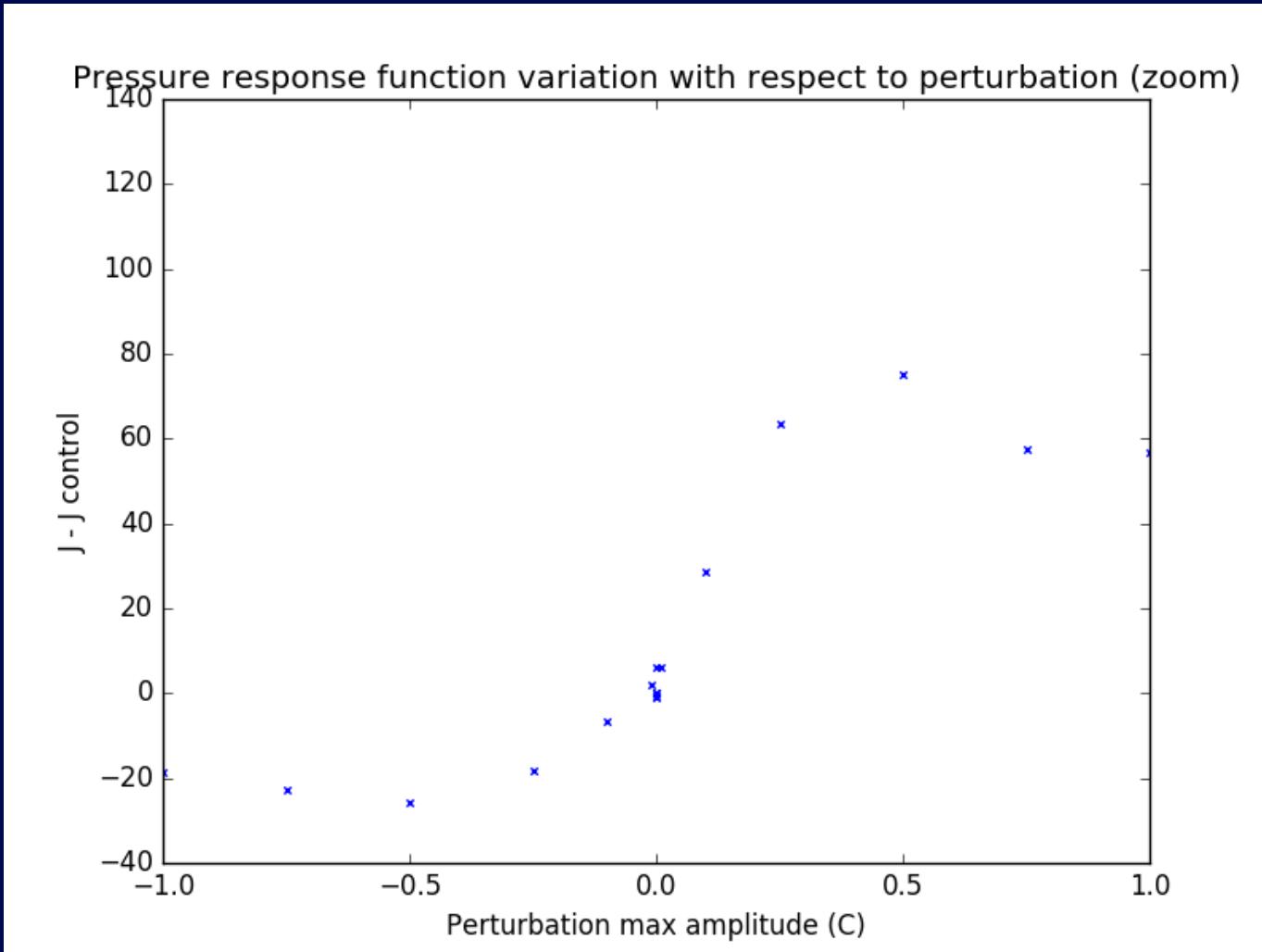


$v$

# Verification of adjoint sensitivities using perturbations: pressure



# Verification of adjoint sensitivities using perturbations: pressure (zoom)



# Current and further work

Dry adjoint sensitivities

No cumulus adjoint sensitivities

Verification of non-linear perturbations with adjoint linear approximation

Verification of non-linear and tangent linear perturbations

# Thank you for your attention!

## Acknowledgements:

COASTEPS  
CGL2017-82868-R

## Programa SOIB – Joves Qualificats



**EUROPEAN UNION**  
EUROPEAN REGIONAL  
DEVELOPMENT FUND  
*"A way to make Europe"*

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i ocupació

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EMPLEO JOVEN  
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